Direct Evidence for Octupole Deformation in $^{146}$Ba and the Origin of Large $E1$ Moment Variations in Reflection-Asymmetric Nuclei

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(Received 13 January 2017; published 12 April 2017)

Despite the more than 1 order of magnitude difference between the measured dipole moments in $^{144}$Ba and $^{146}$Ba, the octupole correlations in $^{146}$Ba are found to be as strong as those in $^{144}$Ba with a similarly large value of $B(E3; 3^- \rightarrow 0^+)$ determined as $48(^{21}_{-29})$ W.u. The new results not only establish unambiguously the presence of a region of octupole deformation centered on these neutron-rich Ba isotopes, but also manifest the dependence of the electric dipole moments on the occupancy of different neutron orbitals in nuclei with enhanced octupole strength, as revealed by fully microscopic calculations.

DOI: 10.1103/PhysRevLett.118.152504

Unlike the electrons in atoms, protons and neutrons are closely bound together in nuclei by the strong nuclear force, occupying quantum levels that can result in different nuclear shapes because of sizable long range multipole-multipole interactions. The studies of these shapes, and of the associated nuclear moments, facilitate our understanding of the origin of simple patterns in such complex quantum many-body systems. Certain isotopes are thought to develop octupole deformation due to strong octupole-octupole interactions present when both types of valence nucleons occupy pairs of single-particle orbitals near the Fermi surface with orbital ($\ell$) and total ($J$) angular momenta differing by $3\hbar$ [1]. There is now experimental evidence to suggest that nuclei with a low-lying negative-parity band of states interleaved with the ground-state positive-parity band and linked by fast $E1$ transitions between the two sequences result from strong octupole correlations. However, because $E3$ transitions are fundamentally hindered in the electromagnetic decay of nuclear states when competing with $E1$ and $E2$ transitions, the presence of strong octupole correlations is often inferred from the observation of large $E1$ transition probabilities. The latter are related to the intrinsic electric dipole moment and are typically obtained from $E1/E2$ intensity ratios, with the $E2$ transition probabilities then being estimated from lifetime measurements of low-spin states or from systematics. A direct experimental determination of the electric octupole moment requires the use of the Coulomb excitation process for the nuclei of interest.

The neutron-deficient radium isotopes around $^{224}$Ra and the neutron-rich barium isotopes centered at $^{146}$Ba have been predicted to belong to the two regions with the strongest octupole correlations [2]. However, large fluctuations, by as much as 2 orders of magnitude for a given spin, in the value of the intrinsic electric dipole moment have been well documented in these two regions [1,3], even though other spectroscopic features, i.e., negative-parity bands located at comparably low excitation energies, strongly suggest the presence of similar octupole strengths. Classically, octupole-deformed nuclei should be characterized by large electric dipole moments proportional to the strength of the octupole correlations [4,5] because of the redistribution of the mass and charge of the protons and neutrons. Interestingly, in the radium isotopes, a minimum occurs in the value of the intrinsic electric dipole moment for $^{222}$Ra, but the magnitude of the octupole strength in this nucleus, as recently quantified through Coulomb excitation with a $^{228}$Ra radioactive beam, is one of the largest in the region [6]. Neutron-rich barium nuclei form another interesting set in terms of studying the relationship between the intrinsic electric dipole and octupole moments [1,7,8]. Specifically, between $^{144}$Ba$_{88}$ and $^{146}$Ba$_{90}$, the electric dipole moments are observed to drop suddenly by more than an order of magnitude [7–9], but the value quickly returns to an enhanced level in $^{148}$Ba$_{92}$ [9]. Furthermore, it
has been pointed out in Ref. [9] that the octupole strength in
$^{146}$Ba may in fact be quenched as this could account for the
presence of a particle alignment at moderate angular
momentum ($I^x \sim 12^+$) in the ground-state band. Clarification
of these issues requires a direct measurement of the $E3$
strength in this nucleus, a challenge until recently because
of its short half-life ($T_{1/2} = 2.2$ s [10]).

Despite the many experimental challenges associated
with measurements of the electric octupole moments in
these nuclei, there is also additional motivation in funda-
mental physics to understand the relation between the
intrinsic electric dipole and octupole moments: the exis-
tence of an atomic electric dipole moment has important
implications for $CP$ violation in the early Universe that
could possibly be responsible for the observed asymmetry
between matter and antimatter [11], herewith signifying
new physics beyond the standard model [12]. In diamag-
netic atoms, a measureable electric dipole moment could be
induced by the so-called Schiff moment, a quantity that can
be enlarged by orders of magnitude by a sizable octupole
moment and is sensitive to details of the charge distribution
[13,14]. Moreover, the contribution of the nuclear intrinsic
electric dipole moment to the Schiff moment is not
ergignificant [14]. Hence, it is important to recognize the
origin and magnitude of nuclear intrinsic moments, espe-
cially the electric dipole moment as it is closely associated
with the nuclear mass and charge distributions. An accurate
estimate of Schiff moments for different nuclei is required
to evaluate the precision of calculations of this quantity and
to compare the limits on $\chi^2$ violation reported by
various experiments involving them.

To determine the octupole strength in $^{146}$Ba, a Coulomb
excitation experiment was performed similar to the one
carried out recently for $^{144}$Ba [15]. The beam of $^{146}$Ba ions
was produced from $^{252}$Cf fission in the CARIBU facility
[16,17] along with the isobaric contaminants $^{146}$La and
$^{146}$Ce, and was charge bred to $q = 28^+$. The $A = 146$
beam was accelerated through the ATLAS accelerator to
659 MeV and was focused onto a $1.1 \text{ mg/cm}^2$ $^{208}$Pb target
(99.86\% enriched). The average $^{146}$Ba beam intensity was
$3 \times 10^3$ ions per second over 12 days. Additional stable
contaminants (with the same $A/q$) included $^{94}$Mo$^{18^+}$,
$^{94}$Zr$^{18^+}$, $^{120}$Sn$^{23^+}$, $^{193}$Ir$^{37^+}$, and $^{198}$Hg$^{38^+}$, but all were
readily separated from the $A = 146$ beam, based on time-
of-flight (TOF) and scattering angle data recorded in the
CHICO2 heavy-ion counter [18] (Fig. 1). This allowed for
a clean $A = 146$ $\gamma$-ray spectrum resulting from Coulomb
excitation (Fig. 2).

In the spectrum of Fig. 2, measured with the GRETINA
$\gamma$-ray tracking array [19], several transitions from $^{146}$Ba are
apparent, especially those belonging to positive-parity
levels in the ground-state band that are excited (and decay)
by $E2$ transitions. The negative-parity levels are populated
less frequently, but the excitation occurs predominantly

\[ \chi^2 \]

through $E3$ transitions and their decay yields provide a
measurement of the corresponding $E3$ matrix elements.

The $\gamma$-ray yields were extracted for two separate scattering
angle ($\theta$) ranges: $30^\circ$–$40^\circ$ and $40^\circ$–$75^\circ$. At lower angles,
it is difficult to isolate the $A = 146$ ions from other beam
contaminants in the TOF spectrum while, at higher $\theta$
values, statistics are insufficient (the cross sections fall
off with the $1/\sin^4(\theta/2)$ Rutherford angular dependence).
The data for each set of angles were analyzed with the
Coulomb excitation least-squares search code GOSIA [20].
Yields were determined for levels up to $10h$ in the ground-
state band and $9h$ in the negative-parity sequence. The
energies of all observed $\gamma$ rays, along with several branch-
ing ratios and level lifetimes, were known from previous
works [7–10]. The latter information proved useful for
constraining the GOSIA fit. The sets of $E1$, $E2$, and $E3$
matrix elements between levels with no previously known
lifetimes were coupled according to the rigid-rotor pre-
scription [21] governed by the individual intrinsic $E\lambda$
moments (see also Refs. [7,15,22]). Once the $\chi^2$ minimum
was found, the rigid-rotor constraint was removed to
properly determine the associated uncertainties, including

\[ E = T \sin^2 \theta \]

FIG. 1. TOF versus scattering angle recorded by CHICO2 in
coincidence with a $\gamma$ ray observed in GRETINA. The $A = 146$
group is readily distinguished from the stable beam contaminants.

FIG. 2. The coincident $\gamma$-ray spectrum obtained by gating on
the $A = 146$ group in the CHICO2 TOF spectrum (Fig. 1). Many
$^{146}$Ba transitions are seen along with lines from the radioactive
isobaric contaminants that were also produced in CARIBU.
corresponds to a deformation present in the ground state \[1\]. This value of \(q\) primarily determined by previous lifetime and/or branching ratio data \([10]\).

Table 1. The experimental \(|\langle I_f^e \mid \hat{M}_j \mid I_i^e \rangle|\) matrix elements \((e \cdot b^{ij})\) based on the GOSIA fit along with new symmetry-conserving configuration-mixing calculations (see text and Ref. \([23]\) for details).

<table>
<thead>
<tr>
<th>(I_i^e \rightarrow I_f^e)</th>
<th>(E)</th>
<th>Experimental</th>
<th>SCCM</th>
</tr>
</thead>
<tbody>
<tr>
<td>(0^- \rightarrow 1^-)</td>
<td>(E1)</td>
<td>0.000223 (10) (^-8)</td>
<td>0.00474</td>
</tr>
<tr>
<td>(1^- \rightarrow 3^-)</td>
<td>(E2)</td>
<td>1.25(5)</td>
<td>1.6</td>
</tr>
<tr>
<td>(0^+ \rightarrow 2^+)</td>
<td>(E2)</td>
<td>1.17(2) (^-3)</td>
<td>1.14</td>
</tr>
<tr>
<td>(2^+ \rightarrow 4^+)</td>
<td>(E2)</td>
<td>1.97(14)</td>
<td>1.90</td>
</tr>
<tr>
<td>(4^+ \rightarrow 6^+)</td>
<td>(E2)</td>
<td>2.35 (+20) (-24)</td>
<td>2.43</td>
</tr>
<tr>
<td>(6^+ \rightarrow 8^+)</td>
<td>(E2)</td>
<td>2.17 (+65) (-33)</td>
<td>2.90</td>
</tr>
<tr>
<td>(0^- \rightarrow 3^-)</td>
<td>(E3)</td>
<td>0.65 (+14) (-20)</td>
<td>0.54</td>
</tr>
<tr>
<td>(2^+ \rightarrow 5^+)</td>
<td>(E3)</td>
<td>1.01 (+61) (-20)</td>
<td>0.87</td>
</tr>
<tr>
<td>(4^+ \rightarrow 7^+)</td>
<td>(E3)</td>
<td>1.25 (+85) (-34)</td>
<td>1.11</td>
</tr>
<tr>
<td>(6^+ \rightarrow 9^+)</td>
<td>(E3)</td>
<td>1.5 (+8) (-12)</td>
<td></td>
</tr>
</tbody>
</table>

\(^a\)Primarily determined by previous lifetime and/or branching ratio data \([10]\).

correlations between matrix elements. In most cases, the uncertainty was primarily limited by the lack of statistics in the measured yields due to the low radioactive beam intensity.

As anticipated, the extracted \(E1\) matrix elements did not display much sensitivity to the data; as mentioned above, the dipole strength was known to be small from earlier work \([7–9]\) and, in fact, the only observed \(\gamma\) rays from \(E1\) decays in the present measurement came from the \(3^-\) and \(5^-\) states. Moreover, the relative sign between the intrinsic \(E1\) and \(E3\) moments was found to also be insensitive to the data. On the other hand, a number of new \(E2\) and \(E3\) matrix elements were well determined from the data (Table I).

The most significant result obtained here is the ground-state \(E3\) matrix element \(|\langle 3_f^e \mid \hat{M}_3 \mid 0_i^e \rangle|\); it is determined to be 0.65 \((+14)\) \((e \cdot b^{3/2})\) and reflects the amplitude of octupole deformation present in the ground state \([1]\). This value corresponds to a \(B(E3; 3^- \rightarrow 0^+)\) reduced transition probability of 48 \((+21)\) W.u., which is essentially the same as the value of 48 \((+25)\) W.u. reported recently for \(^{146}\)Ba \([15]\). This new result supports the long-standing prediction that \(^{146}\)Ba is indeed one of the isotopes with strong octupole collectivity \([24]\).

The persistence of this strong collectivity between \(^{144}\)Ba\(_{88}\) and \(^{146}\)Ba\(_{90}\) confirms that the drastic reduction in electric dipole moment between the two isotopes is not the result of quenched octupole strength, as suggested by the high-spin behavior of \(^{146}\)Ba. The sudden band alignments in \(^{146}\)Ba pointed out in Ref. \([9]\) are then most likely the result of a crossing between yrast and yrare bands predicted in this mass region sometime ago \([28,29]\). It should be noted that alternative explanations have also been proposed. These include a transition to a more reflection-symmetric shape at moderate spin \([30]\), and a description in terms of a condensate of rotationally aligned octupole phonons \([31,32]\). Concerning the latter, however, it should be mentioned that while the interleaved sequences of opposite parity are consistent with the proposed picture, the absence of strong \(E1\) linking transitions associated with multioctupole phonon excitations at higher spins is not.

Over the past three decades, extensive theoretical efforts have been devoted to understanding the variation of the \(E1\) transition strengths observed in nuclei near \(^{146}\)Ba and \(^{224}\)Ra \([33–41]\). It is generally believed that the observations are the result of the relation between octupole collectivity and the nonuniform distribution of protons and neutrons. This was first shown within the framework of a macroscopic-microscopic approach where the experimental \(E1\) transition strengths could be described \([33,37]\). Early self-consistent Hartree-Fock-Bogoliubov (HFB) calculations with the Gogny interaction were also able to reproduce the very low values of the dipole moment \(D_0\) in \(^{224}\)Ra and \(^{146}\)Ba \([36,38]\). However, all of these models predicted that the nuclei under study are reflection asymmetric, and argued that this is at the core of the observed variations. Thus, the recently measured strong octupole collectivity in \(^{144}\)Ba \([15]\) and \(^{146}\)Ba (Table I) provides an important validation of this interpretation.

More recently, microscopic self-consistent methods have been improved by including beyond-mean-field correlations. These developments provide an explanation of the microscopic origin of octupole collectivity and study the impact of octupole correlations on both ground-state properties and electromagnetic transitions. To explore in \(^{146}\)Ba this phenomenon of a strong octupole collectivity accompanied by a much reduced electric dipole moment, a theoretical model based on mean field HFB intrinsic wave functions has been used with a symmetry-conserving configuration-mixing method (SCCM). The model assumes that only the axially symmetric quadrupole \((Q_{20})\) and octupole \((Q_{30})\) degrees of freedom are relevant (collectively referred to as \(Q\)). A set of constrained HFB states \(|Q\rangle\), subsequently projected onto good angular momentum, parity, and particle number (the corresponding states are denoted as \(|\Phi^{J=\pi}(Q)\rangle\) is used as a variational subspace. Linear combinations of the above states \(|\Psi_{J}^{\pi}(Q)\rangle = \sum_{\sigma} f_{\sigma}^{J} \langle Q | \Phi^{J=\pi}(Q) \rangle \rangle\) are used in the spirit of the generator coordinate method (GCM) to obtain the low-lying collective spectrum (see Ref. \([23]\) for a recent account and an application to \(^{146}\)Ba). The interaction generating the intrinsic states is the well-known Gogny D1S force \([42]\). The
The deformation parameters $\beta_2$ and octupole $\beta_3$ deformation parameters are defined as $\beta_2 \equiv 4\pi(q_r Y_{00})/\beta_0$ with $r_0 = 1.2$ fm and $A$ being the mass number. Dashed (solid) contour lines are separated by 0.5 (2.0) MeV.

The HFB potential energy surface as a function of the collective amplitudes $F_{\lambda,\Sigma}(Q)$ is given in Fig. 3 for $^{146}$Ba. Note that the potential energy is symmetric under the change of sign of $\beta_3$ due to the parity symmetry of the nuclear interaction. A reflection-asymmetric, absolute minimum is obtained at $\beta_2 = 0.21$ and $\beta_3 = \pm 0.1$. The shape of the $F_{\lambda,\Sigma}$ collective amplitudes is mainly driven by the intrinsic potential energy surface. As a consequence, the $F_{\lambda,\Sigma}$ amplitudes for $^{146}$Ba are concentrated around those minima as seen in Fig. 4 where they are compared with those for $^{144}$Ba and $^{148}$Ba. In the three nuclei, the $1^-$ and $0^+$ collective amplitudes have a very large overlap, characteristic of strong octupole correlations. The energy of the $1^-$ state is well reproduced; however, the ground-state and negative-parity sequences are characterized by a smaller moment of inertia than observed, due to limitations discussed in Ref. [23].

The electromagnetic transition strengths have been computed without invoking effective charges or uncontrolled approximations. The calculated values are compared with the experimental data in Table I. There is fair agreement between the calculated and measured $E1$ matrix elements, including the strong $B(E1)$ strengths between the $3^-$ and $0^+$ and the much quenched $E1$ between the $1^-$ and $0^+$ states. In the present microscopic framework, the $B(E1)$ transition strength is proportional to the square of the overlap of the dipole operator between the initial $1^-$ and final $0^+$ states. There are two basic ingredients entering the required overlap [see Eq. (4) of Ref. [23]]. One is the structure of the collective wave functions $F_{\lambda,\Sigma}(Q)$, and the other is the overlap between the projected intrinsic states $|\Phi_{\lambda,\Sigma}(Q)\rangle$. Because the values of $F_{\lambda,\Sigma}(Q)$, as shown in Fig. 4, exhibit little variation with neutron number in the three Ba isotopes, the sudden drop of $B(E1)$ in $^{146}$Ba has to be associated with the overlap of the dipole operator between the projected intrinsic states $|\Phi_{\lambda,\Sigma}(Q)\rangle$.

Specifically, the calculations indicate that the dipole moment changes from positive values in $^{144}$Ba, to nearly zero values in $^{146}$Ba, and finally to negative values in $^{148}$Ba. Hence, the changes in $E1$ strengths with neutron number are associated with changes in the intrinsic dipole moment linked to the evolving mean field. A similar conclusion was reached in Ref. [38].

The behavior of the dipole moment with neutron number in these Ba isotopes can further be traced back to the occupation of specific single-particle states near the Fermi surface. Considering the evolution of the single-particle energies with $\beta_3$ in Fig. 5, three neutron orbitals are of interest with $K^\pi$ quantum numbers $3/2^-$, $5/2^-$, and $1/2^+$. These are of $h_{9/2}$, $f_{7/2}$, and $i_{13/2}$ spherical parentage, respectively. The three states are empty in $^{144}$Ba, but have

![FIG. 3. The HFB potential energy surface. Axial quadrupole ($\beta_2$) and octupole ($\beta_3$) deformation parameters are defined as $\beta_2 \equiv 4\pi(q_r Y_{00})/\beta_0$ with $r_0 = 1.2$ fm and $A$ being the mass number. Dashed (solid) contour lines are separated by 0.5 (2.0) MeV.](image1)

![FIG. 4. Collective amplitudes corresponding to $^{144}$Ba (left), $^{146}$Ba (middle), and $^{148}$Ba (right).](image2)

![FIG. 5. Neutron single-particle energies as a function of $\beta_2$ (left) and as a function of $\beta_3$ (right) for $^{146}$Ba. The right panel is calculated with a constant value of $\beta_3 = 0.2$ (ground-state value) starting with $\beta_3 = 0$ at the central vertical axis. A thick dotted line shows the Fermi level. The single-particle energy as a function of $\beta_3$ is used to justify the spherical orbital assignments and parities of the relevant neutron orbitals (see text for details).](image3)
significant respective occupancies of $v^2 = 0.4$, $v^2 = 0.27$, and $v^2 = 0.20$ in $^{146}$Ba. As visualized in Fig. 4 of Ref. [38], their occupation results in a contribution to the dipole moment that almost cancels that by the protons. As the occupancies increase further with two additional neutrons in $^{148}$Ba, the (total) dipole moment changes sign and returns to a sizable value.

To summarize, the $E3$ strength in short-lived $^{146}$Ba was measured directly by multistep Coulomb excitation with GRETINA and CHICO2. The long-standing prediction of an enhanced octupole collectivity was verified. The data also provide firm experimental evidence that the large drop of the $B(E1)$ value is not the result of quenched octupole collectivity in $^{146}$Ba. Such a collectivity is well reproduced by the SCCM model with the Gogny energy density functional, and the variation in $E1$ strength between isotopes is associated with changes in the neutron occupancy of high-$j$, low-$K$ orbitals located near the Fermi surface. The present results help validate the general character of the microscopic origin of large variations in electric dipole moments in the reflection-asymmetric nuclear potential, and they represent an important confirmation of such effects in the Ba region of neutron-rich nuclei.

This material is based upon work supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under Contract No. DE-AC02-06CH11357 (ANL). Work at LLNL and INL is supported by the U.S. DOE under respective Contracts No. DE-AC52-07NA27344 and No. DE-AC07-05ID14517. GRETINA was funded by the U.S. DOE, Office of Science, Office of Nuclear Physics under respective Contracts No. DE-AC02-07NA27344 and No. DE-AC02-05CH11231 (LBNL). This research used resources of ANL’s ATLAS facility, which is a DOE Office of Science User Facility. The work of L. M. R. was supported by Spanish Grants No. FIS2012-34479-P MINECO, No. FPA2015-65929-P MINECO, and No. FIS2015-63770-P MINECO, and the work of T. R. R. by Spanish Grants No. FIS-2014-53434-P MINECO and Programa Ramón y Cajal 2012 No. 11420.

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24 Recently, a new evaluation on $^{146}$Ba was published [25] that identifies a $\gamma$-ray transition with strong intensity connecting the $3_1^1$ level to the ground state. However, the details surrounding the measurement responsible for this result are not easily accessible while the corresponding $B(E3)$ is unphysically high (≈1600 W.u.). The nonobservation of this $\gamma$-ray in Refs. [8,9,26,27] is consistent with the present result.


