

SUSY seesaw: interplay of low energy and LHC observables

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based on work with A. Abada, J. C. Romão and A. M. Teixeira

March 29, 2012

Motivation (1/11)

Experimental discovery of 3 very light ν_L species

- ▶ Super-Kamiokande: evidence for ν oscillations in 1998
- ▶ Oscillations \Rightarrow Misalignment between **Mass** and **Flavour** basis ($W^- l_i^\dagger \nu_i$) \Rightarrow **massive ν_L**
- ▶ Neutrino Oscillations \Rightarrow **Neutral Lepton Flavour Violation**
- ▶ Potentially inducing **cLFV?**

Since then

- ▶ 5 out of 7 (or 9) neutrino oscillation parameters determined to good precision

$$\Delta m_{21}^2, |\Delta m_{31}^2|, \theta_{12}, \theta_{23}, \theta_{13}$$

- ▶ Missing:

$$\delta, \phi_1, \phi_2, m_\nu \quad (\text{plus hierarchy})$$

- ▶ Very recently (Daya Bay $\bar{\nu}_e \rightarrow \bar{\nu}_e$):

$$\theta_{13} \neq 0 \text{ at } 5.2\sigma \text{ \& b.f.p. } \theta_{13} \approx 9^\circ$$

Massive ν SM extensions (2/11)

Naive ν_R -extended SM

- ▶ Unnaturally small Yukawa couplings \Leftarrow Smallness should be related to a symmetry enhancement in the vanishing couplings limit! ('t-Hooft)
- ▶ Very suppressed cLFV observables: $\propto m_\nu/M_W \sim 0$, e.g.

$$BR(l_i \rightarrow l_j \gamma) < 10^{-53}$$

The seesaw mechanism:

- ▶ Assumes ν is a Majorana particle
- ▶ Naturalness: smallness of m_ν/v with $\mathbf{Y}^\nu \sim \mathcal{O}(1)$ justified by breaking Lepton Number Conservation (or $\bar{B} - L$) at a very high energy scale! (close to GUT?)

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E.g. **Fermionic** seesaws (Type-I and -III): $Y_{ij}^\nu H_u L_i F_j \rightarrow$

$$\rightarrow \left(Y^\nu \frac{1}{\Lambda} Y^{\nu T} \right)_{ij} (H_u L_i)(H_u L_j) \xrightarrow{\text{EWSB}} \boxed{m_\nu \simeq -Y^\nu \frac{v^2}{\Lambda} Y^{\nu T}}$$

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- ▶ Appealing scenario to explain the present BAU as generated by Leptogenesis from a B-symmetric big-bang

SM seesaw or SUSY seesaw? (3/11)

SM+Seesaw?

- ▶ If motivated by $Y_\nu \sim \mathcal{O}(1)$ ($\Leftrightarrow \Lambda > 10^{10}$ GeV), it can aggravate the Higgs “fine tuning” problem!
- ▶ Hard to reconstruct the parameters of the underlying mechanism and to falsify a particular seesaw mechanism
- ▶ Does not solve the Hierarchy problem nor does it provide a dark matter candidate
- ▶ Still, very suppressed cLFV since at low energy all LFV is as in the SM

SUSY+Seesaw?

- ▶ Solves the Hierarchy problem and ameliorates the Higgs “fine tuning” problem
- ▶ Provides dark matter candidates, the most popular being the lightest neutralino (χ_1^0)
- ▶ Potentially observable cLFV since the seesaw also leaves imprint upon the charged slepton sector!

SUSY seesaw assumptions (4/11)

Choose SUSY+Seesaw type-I

- ▶ Avoid CP and Flavour problems \Rightarrow **cMSSM**

\Rightarrow Universal soft-breaking masses

& tri-linear soft-breaking (proportional to Yukawas)

$$\text{Sleptons: } m_{\tilde{L}}^2 = m_{\tilde{E}}^2 = m_0^2 \mathbf{1}, \quad A^l = A_0 Y^l \quad (@ \text{ GUT})$$

- ▶ Mimicking the light-neutrinos: three species of $\hat{N} \sim \nu_L^c \oplus \tilde{\nu}_R^\dagger$

$$W_{\text{seesaw-I}} = \frac{1}{2} \hat{N} M_N \hat{N} - \hat{H}_u \hat{L} Y^\nu \hat{N}$$

enlarging the soft-breaking sector

$$-\mathcal{L}_{\text{seesaw-I}}^{\text{soft}} = \tilde{\nu}_R^\dagger m_{\tilde{\nu}_R}^2 \tilde{\nu}_R + \left(\frac{1}{2} \tilde{\nu}_R^\dagger B_\nu \tilde{\nu}_R^\dagger - H_u \tilde{L} A^\nu \tilde{\nu}_R^\dagger + h.c. \right)$$

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$$Y^\nu \sim \mathcal{O}(1) \text{ \& } m_{\text{soft}} \lesssim \mathcal{O}(\text{TeV})$$

$$\Rightarrow M_N \gg B_\nu \Rightarrow \tilde{\nu}_R^\dagger (B_\nu + M_N) \tilde{\nu}_R^\dagger \simeq \tilde{\nu}_R^\dagger M_N \tilde{\nu}_R^\dagger$$

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Extending minimal supergravity inspired SUSY-breaking

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Y^ν is the unique source of LFV!

SUSY seesaw consequences (5/11)

At low energies:

- ▶ m_ν , after EWSB, from the unique dimension five operator
- ▶ Higher dimension operators quite suppressed by naturalness requirements on Y^ν
- ▶ Deviation from mSUGRA-inspired flavour-blindness @ GUT due to RGE induced effects

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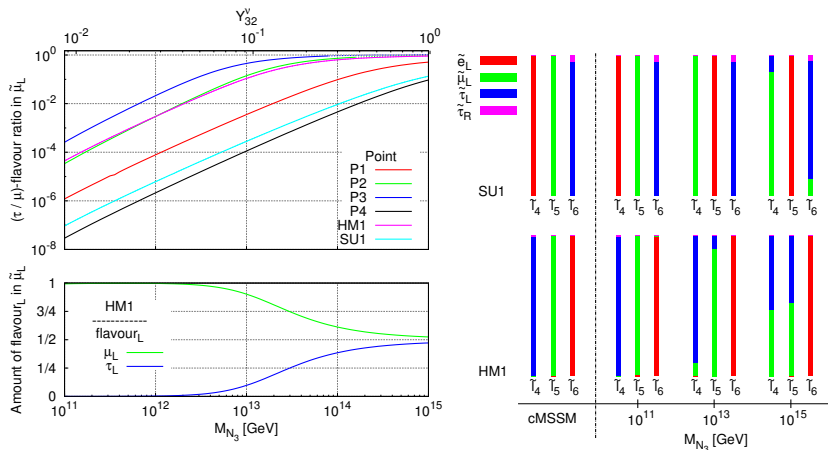
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Slepton flavour mixing proportional to Y^ν

$$Y^{\nu T} v_u \simeq i\sqrt{M_N} R \sqrt{m_\nu} U_{MNS}^\dagger$$

Example of Slepton Flavour Mixing (6/11)



- ▶ Increasing the seesaw scale \rightarrow natural $Y^\nu \Rightarrow$ slepton flavour mixing increases
- ▶ Usually: two-(flavour, left-handed) slepton mass eigenstates

cLFV observables (7/11)

At the **LHC** we expect to

- ▶ Discover SUSY!
- ▶ Study the Slepton sector via $\chi_2^0 \rightarrow \tilde{\ell}^\pm \ell^\mp \rightarrow \ell^\pm \ell^\mp \chi_1^0$

$$\underline{\text{Slepton Mass Splittings (SMS)}}: \quad \frac{\Delta m}{m}(\tilde{\ell}_i, \tilde{\ell}_j) \sim \mathcal{O}(0.1\%)$$

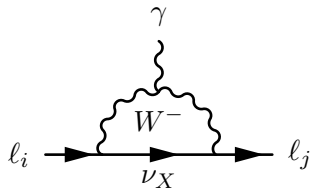
- ▶ cLFV decays $\chi_2^0 \rightarrow \ell_i^+ \ell_j^- \chi_1^0$

Low energy experiments we currently **know** and **expect** (e.g.)

$BR(\mu \rightarrow e\gamma)$	$< 2.4 \times 10^{-12}$ (MEG @ PSI, 2011)	10^{-13} (MEG)
$BR(\tau \rightarrow \mu\gamma)$	$< 4.5 \times 10^{-8}$ (Belle @ KEKB, 2006)	10^{-9} (SuperB)
$CR(\mu - e, \text{Ti})$	$< 4.3 \times 10^{-12}$ (SINDRUM II @ PSI, 1993)	10^{-16} (Mu2e @ Fermilab)
		10^{-18} (PRISM/PRISME @ J-PARC)

SUSY seesaw cLFV (8/11)

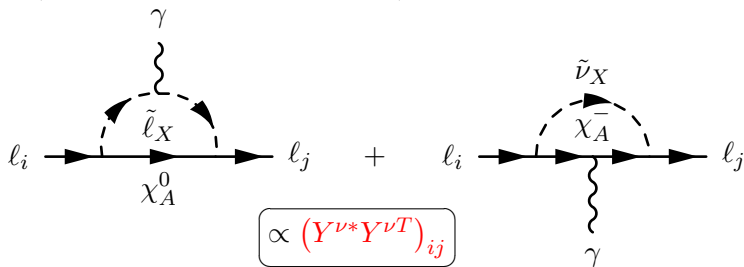
- ▶ cLFV at low energy: $\text{SM}_{\nu_R} \rightarrow \text{SUSY seesaw}$
(SM+neutrino oscillations)



$$\propto \left(U_{MNS}^* \frac{m_\nu^2}{M_W^2} U_{MNS}^T \right)_{ij}$$

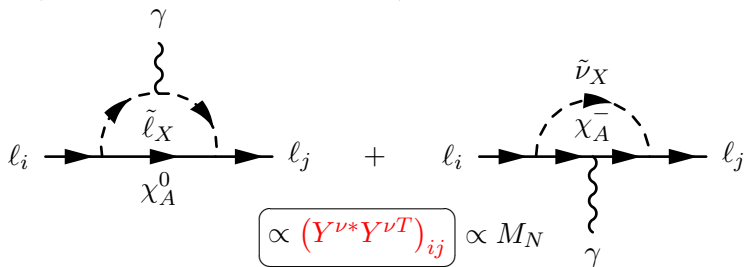
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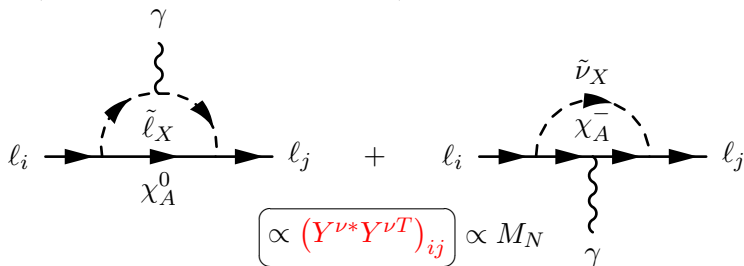
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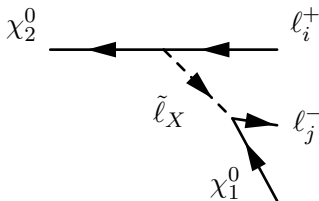


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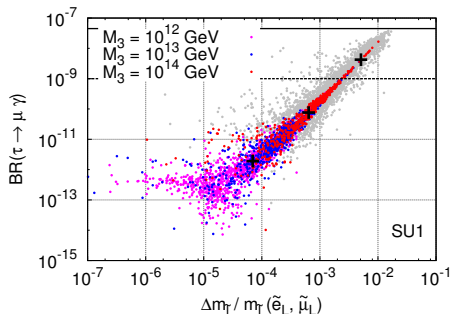
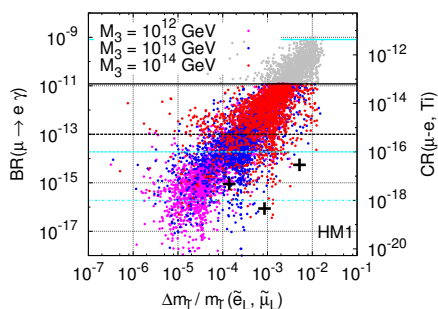
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- cLFV at the LHC

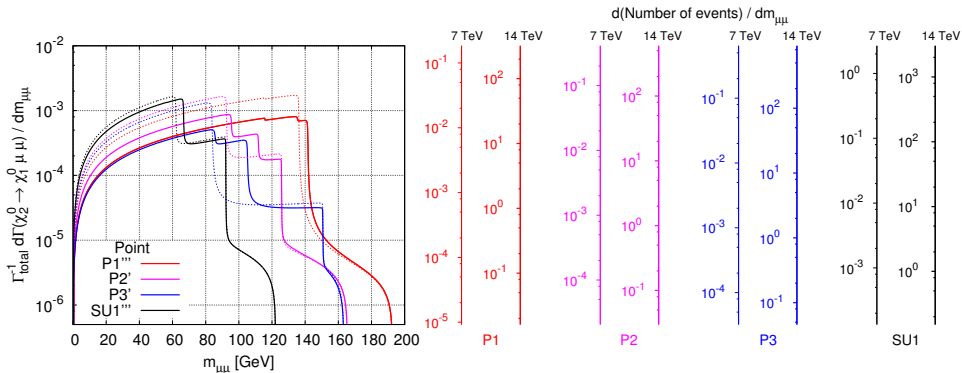


SMS and low energy cLFV interplay (9/11)



- ▶ HM1: If slepton mass splittings (SMS) are observed at LHC \Rightarrow MEG should observe $\mu \rightarrow e \gamma$ & $M_3 \approx 10^{14}$ GeV (dependent on θ_{13})
- ▶ HM1: Given $\theta_{13} \approx 9^\circ$, observation of SMS would be incompatible with present bounds on $BR(\mu \rightarrow e \gamma)$!
- ▶ SU1: Tight correlation between SMS and low energy cLFV

Edges in leptonic invariant mass distributions (10/11)



- ▶ Two mass eigenstates \Rightarrow 2-edges

$$\chi_2^0 \rightarrow \tilde{\mu}_{L,R}^{\pm} \mu^{\mp} \rightarrow \mu^{\pm} \mu^{\mp} \chi_1^0$$

- ▶ 3-edges \Rightarrow (in)direct evidence of sleptonic cLFV

$$\chi_2^0 \rightarrow \begin{pmatrix} \tilde{\mu}_{L,R}^{\pm} \\ \tilde{\tau}_2^{\pm} \end{pmatrix} \mu^{\mp} \rightarrow \mu^{\pm} \mu^{\mp} \chi_1^0$$

Conclusions (11/11)

Assuming minimal supergravity inspired SUSY breaking + the standard natural seesaw

- ▶ A tight correlation exists between low energy cLFV within future sensitivity and potentially observable slepton mass splittings at the LHC
- ▶ Multiple edges in flavour conserving di-leptonic invariant mass distribution already allow to hint towards sizable charged (s)lepton flavour violation

We have also conducted a similar analysis for the type-III
Work in progress: prospects for the SUSY seesaw in a e^+e^- or e^-e^- Linear Collider

Backup Slides

Point	m_0 (GeV)	$M_{1/2}$ (GeV)	A_0 (TeV)	$\tan \beta$
P1	110	528	0	10
P2	110	471	1	10
P3	137	435	-1	10
P4	490	1161	0	40
P5-HM1	180	850	0	10
P6-SU1	70	350	0	10

Table: mSUGRA benchmark points selected for the LFV analysis: m_0 , $M_{1/2}$ (in GeV) and A_0 (in TeV), as well as $\tan \beta$. For all points we take $\mu > 0$. Points P5-HM1 and P6-SU1 are LHC CMS- and ATLAS-proposed benchmark points.

Point	M_{N_1} (GeV)	M_{N_2} (GeV)	M_{N_3} (GeV)	θ_{13}
P'	10^{10}	5×10^{10}	5×10^{13}	0.1°
P''	10^{10}	10^{12}	5×10^{12}	1°
P'''	10^{10}	10^{12}	10^{15}	0.1°

Table: Seesaw benchmark points. For the remaining parameters we have taken $R = 1$, and $\varphi_1 = \varphi_2 = \delta = 0$.

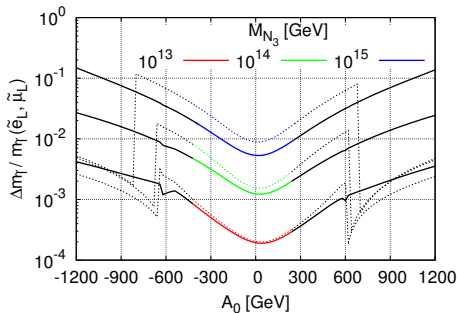


Figure: Comparison between “real” (dashed lines) and “effective” (full) slepton mass differences ($\tilde{e}_L - \tilde{\mu}_L$), normalised to the average $\tilde{e}_L, \tilde{\mu}_L$ mass, as a function of A_0 (in GeV). We have considered $R = 1$, $\theta_{13} = 0.1^\circ$, $M_{N_1} = 10^{10}$ GeV, $M_{N_2} = 10^{11}$ GeV, taking three distinct values for $M_{N_3} = 10^{13}$ GeV (red), $M_{N_3} = 10^{14}$ GeV (green) and $M_{N_3} = 10^{15}$ GeV (blue). The mSUGRA parameters have been set as for point P1 (except for $|A_0| \leq 1.2$ TeV). Black lines denote points excluded due to the violation of at least one experimental and/or observational constraint.

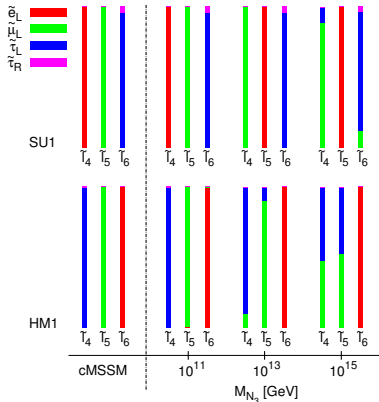
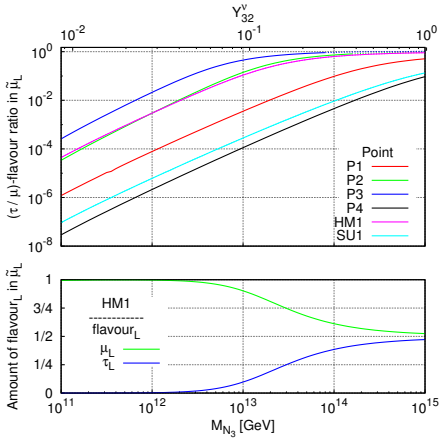


Figure: On the left, τ/μ flavour ratio in $\tilde{\mu}_L$ mass eigenstate as a function of M_{N_3} (in GeV). For the mSUGRA benchmark points of Table 1, we set $R = 1$, $\theta_{13} = 0.1^\circ$ (with $\delta = \varphi_{1,2} = 0$), and take $M_{N_1} = 10^{10}$ GeV, $M_{N_2} = 10^{11}$ GeV. On the upper axis we display the values of Y_{32}^ν . The secondary panel illustrates $|R_{5\mu_L}^{\tilde{L}}|^2$ and $|R_{5\tau_L}^{\tilde{L}}|^2$ for the same M_{N_3} interval. On the right we depict the flavour content of the 3 heavier mass eigenstates: red - \tilde{e}_L , green - $\tilde{\mu}_L$, blue (magenta) - $\tilde{\tau}_{L(R)}$, for P5-HM1 and P6-SU1, illustrating both the cMSSM case (on the far left) and the type-I seesaw, for three values of M_{N_3} (with the remaining seesaw parameters as before).

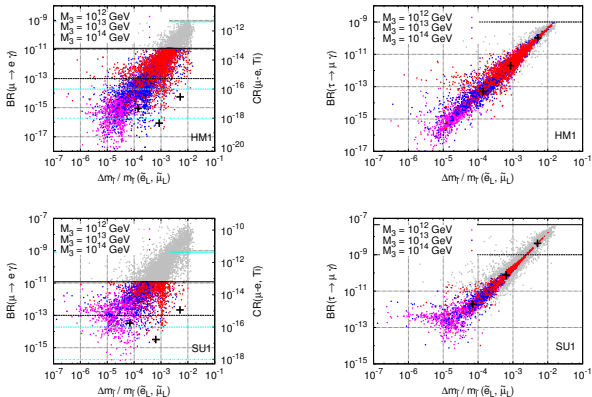


Figure: Upper left (right) panel: $\text{BR}(\mu \rightarrow e\gamma)$ ($\text{BR}(\tau \rightarrow \mu\gamma)$) on the left y-axis as a function of the mass difference $\tilde{e}_L - \tilde{\mu}_L$, normalised to the average $\tilde{e}_L, \tilde{\mu}_L$ mass, for seesaw variations of point P5-HM1. We display the corresponding predictions of $\text{CR}(\mu - e, \text{Ti})$ on the secondary right y-axis. Lower panels: same as above, but for point P6-SU1. Horizontal lines denote the corresponding current bounds/future sensitivities. The distinct coloured regions correspond to three different values of $M_{N_3} = \{10^{12}, 10^{13}, 10^{14}\}$ GeV. The remaining parameters were set as $M_{N_1} = 10^{10}$ GeV, $M_{N_2} = 10^{11}$ GeV, $\theta_{13} = 0.1^\circ$ and the complex R matrix angles have been randomly varied as $|\theta_i| \in [0, \pi]$, and $\arg(\theta_i) \in [-\pi, \pi]$. The crosses correspond to the different seesaw benchmark points: from smaller to larger mass splittings one has HM1'' (SU1''), HM1' (SU1'), HM1''' (SU1'''), for the upper (lower) panels.

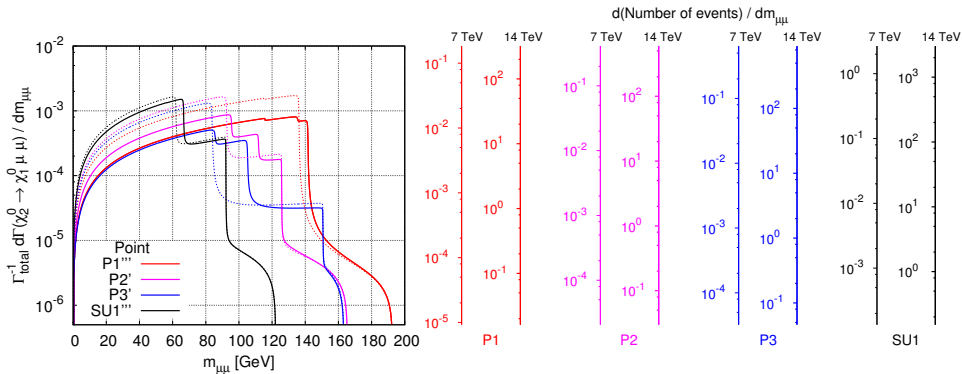


Figure: $\text{BR}(\chi_2^0 \rightarrow \mu\mu\chi_1^0)$ as a function of the di-muon invariant mass $m_{\mu\mu}$ (in GeV) for different SUSY seesaw points (see Tables 1 and 2). Upper panel: P1''' (red), P2' (pink), P3' (blue) and P6-SU1''' (black). Dotted (coloured) lines denote in both panels the curves for the corresponding cMSSM case. Secondary (right) y-axes denote the corresponding expected number of events for $\sqrt{s} = 7$ TeV and 14 TeV, respectively with $\mathcal{L} = 1 \text{ fb}^{-1}$ and $\mathcal{L} = 100 \text{ fb}^{-1}$.