

Minimal Flavor Violation with a Strong Higgs Dynamics

Juan Yepes



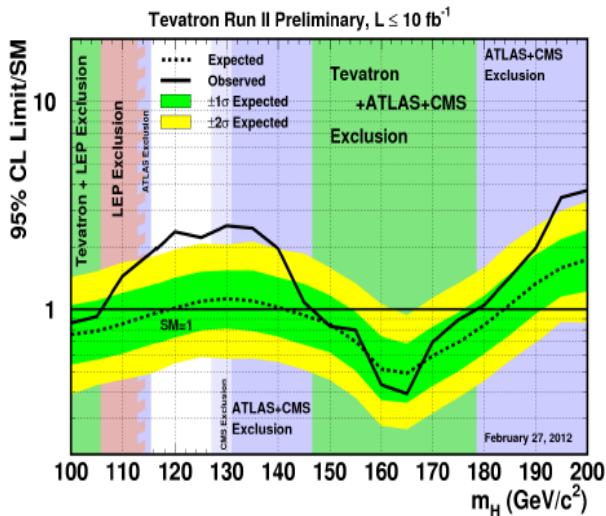
Instituto de Física Teórica, IFT-UAM/CSIC
Universidad Autónoma de Madrid

Invisibles ITN pre-meeting

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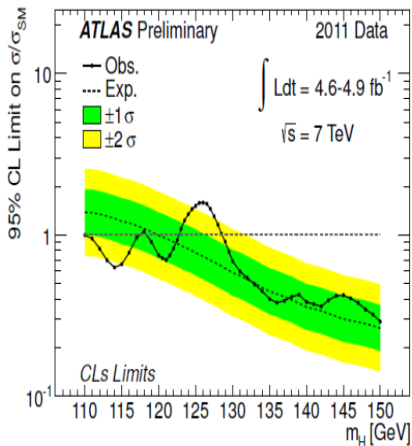
Based on: [Alonso, Gavela, Merlo, Rigolin & JY, 1201.1511 \[hep-ph\]](#)

CDF + DØ

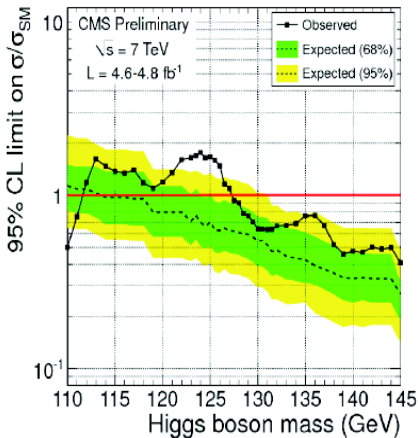


$$115 < m_H(\text{GeV}) < 135$$

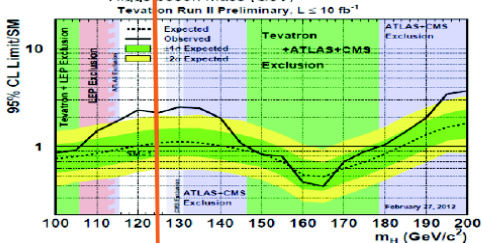
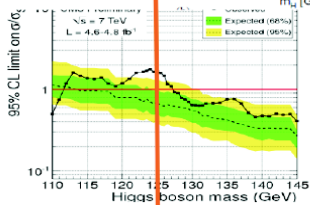
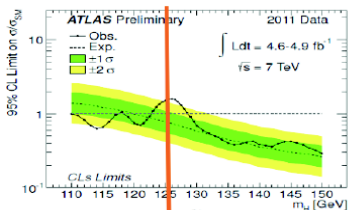
ATLAS & CMS



$$122.5 < m_H(\text{GeV}) < 129$$



$$114.4 < m_H(\text{GeV}) < 127.5$$



Blondel resume
 Moriond 2012

IF NO HIGGS THERE...

IF NO HIGGS THERE... → m_H up to TeV → STRONG INTERACTING
REGIME

Kaplan & Georgi '84

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IF THERE , AND NOTHING ELSE UP TO TeV...

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IF THERE , AND NOTHING ELSE UP TO TeV... → STILL STRONG
DYNAMICS

Giudice, Grojean, Pomarol & Rattazzi '07

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IF THERE , AND NOTHING ELSE UP TO TeV... → STILL STRONG
DYNAMICS

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Whether it is at the TeV or at 125 GeV

I will assume that the HIGGS DYNAMICS IS STRONG

What about **FLAVOR** in this context??...

MINIMAL FLAVOR VIOLATION (MFV)

Ansatz: Yukawa couplings are the unique sources for flavor effects at low energy in SM and beyond. Chivukula & Georgi '87.

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recovering \mathcal{G}_f
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Minimally flavour violating dimension six operator	main observables	Λ_f [TeV]	
		-	+
$\mathcal{O}_0 = \frac{1}{2}(\bar{Q}_L \lambda_{FC} \gamma_\mu Q_L)^2$	$\epsilon_K, \Delta m_{B_d}$	6.4	5.0
$\mathcal{O}_{F1} = H^\dagger (\bar{D}_R \lambda_d \lambda_{FC} \sigma_{\mu\nu} Q_L) F_{\mu\nu}$	$B \rightarrow X_s \gamma$	9.3	12.4
$\mathcal{O}_{G1} = H^\dagger (\bar{D}_R \lambda_d \lambda_{FC} \sigma_{\mu\nu} T^a Q_L) G_{\mu\nu}^a$	$B \rightarrow X_s \gamma$	2.6	3.5
$\mathcal{O}_{\ell 1} = (\bar{Q}_L \lambda_{FC} \gamma_\mu Q_L)(\bar{L}_L \gamma_\mu L_L)$	$B \rightarrow (X) \ell \bar{\ell}, \quad K \rightarrow \pi \nu \bar{\nu}, (\pi) \ell \bar{\ell}$	3.1	2.7 *
$\mathcal{O}_{\ell 2} = (\bar{Q}_L \lambda_{FC} \gamma_\mu \tau^a Q_L)(\bar{L}_L \gamma_\mu \tau^a L_L)$	$B \rightarrow (X) \ell \bar{\ell}, \quad K \rightarrow \pi \nu \bar{\nu}, (\pi) \ell \bar{\ell}$	3.4	3.0 *
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$\mathcal{O}_{q5} = (\bar{Q}_L \lambda_{FC} \gamma_\mu Q_L)(\bar{D}_R \gamma_\mu D_R)$	$B \rightarrow K \pi, \quad \epsilon'/\epsilon, \dots$	~ 1	

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$$\Rightarrow \Lambda_f \sim \text{TeV}$$

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Strongly interacting Higgs $\lambda \sim 1 \Rightarrow$ **unsuppressed longitudinal $W - Z$ components emission**



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→ Model independent: effective lagrangian approach

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$$\Phi = \begin{pmatrix} \phi^\dagger \\ \phi^0 \end{pmatrix} \quad \rightarrow \quad \mathbf{U} = e^{i\hat{\pi}/v} \text{ (no mass dimension!)}$$
$$\hat{\pi} = \begin{pmatrix} \pi^0 & \sqrt{2}\pi^+ \\ \sqrt{2}\pi^- & -\pi^0 \end{pmatrix}$$

Low cost of π -fields emission!

What changes if the Higgs has strong interacting dynamics?

- ▶ Tower of operators becomes...



STRONG HIGGS DYNAMICS

+

MINIMAL FLAVOR VIOLATION

$$\mathcal{O}_1 \sim \bar{\psi}_\alpha \gamma^\mu \left[\mathbf{U} \tau_3 \mathbf{U}^\dagger (\mathcal{D}_\mu \mathbf{U}) \mathbf{U}^\dagger + (\mathcal{D}_\mu \mathbf{U}) \tau_3 \mathbf{U}^\dagger \right] \psi_\beta$$

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STRONG HIGGS DYNAMICS + MINIMAL FLAVOR VIOLATION

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\mathcal{O}_4 is a CP-ODD op.! \rightarrow Natural CP @ LO!!

STRONG HIGGS DYNAMICS

+

MINIMAL FLAVOR VIOLATION

$$\delta\mathcal{L}_{d_X=4} = -\frac{g}{\sqrt{2}} \left[W^{\mu+} \bar{U}_L \gamma_\mu (a_W + i a_{CP}) (\mathbf{y}_U^2 V + V \mathbf{y}_D^2) D_L + h.c. \right] +$$

$$-\frac{g}{2c_W} Z^\mu \left[a_Z^u \bar{U}_L \gamma_\mu (\mathbf{y}_U^2 + V \mathbf{y}_D^2 V^\dagger) U_L + a_Z^d \bar{D}_L \gamma_\mu (\mathbf{y}_D^2 + V^\dagger \mathbf{y}_U^2 V) D_L \right]$$

$$a_Z^u \equiv a_1 + a_2 + a_3,$$

$$a_W \equiv a_2 - a_3,$$

$$a_Z^d \equiv a_1 - a_2 - a_3,$$

$$a_{CP} \equiv -a_4.$$

ϵ_K vs. $R_{BR/\Delta M}$

a^d s from $a_i \mathcal{O}_i$

$$R_{BR/\Delta M} = \frac{BR(B^+ \rightarrow \tau^+ \nu)}{\Delta M_{B_d}}$$

$a_{CP} = \pm 0.1$	\rightarrow	$\delta \epsilon_K \approx 1.1\%$,	$\delta R_{BR/\Delta M} \approx -1.4\%$,
$a_W = 0.1(-0.1)$	\rightarrow	$\delta \epsilon_K \approx +26\%(-19\%)$,	$\delta R_{BR/\Delta M} \approx -25\%(+30\%)$,
$a_Z^d = \pm 0.1$	\rightarrow	$\delta \epsilon_K \approx 124\%$,	$\delta R_{BR/\Delta M} \approx -62\%$.

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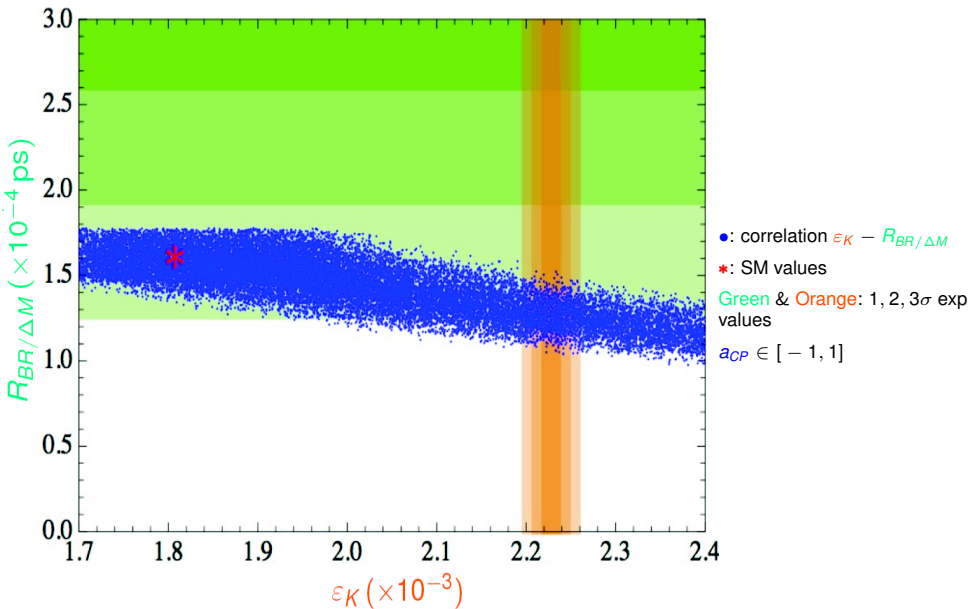
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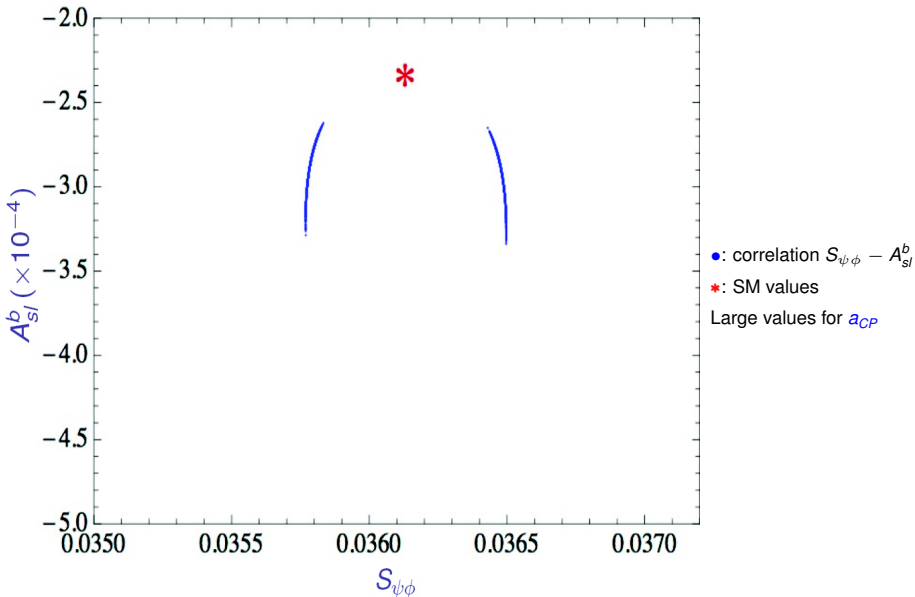
$$\epsilon_K \uparrow (\approx \epsilon_K^{\text{exp}} \text{ \& } S_{\psi K_S} \approx S_{\psi K_S}^{\text{exp}}) \text{ \& } R_{BR/\Delta M} \downarrow$$

\Rightarrow SHD + MFV able to remove $\epsilon_K - S_{\psi K_S}$ anomaly, but not the SM tension for $BR(B^+ \rightarrow \tau^+ \nu)$

ϵ_K vs. $R_{BR/\Delta M}$ from \mathcal{O}_4



$S_{\psi\phi}$ vs. A_{sl}^b from \mathcal{O}_4



STRONG HIGGS DYNAMICS
+
MINIMAL FLAVOR VIOLATION



- ▶ Different MFV phenomenology for the perturbative Higgs and the strong interacting regime, e.g., \mathcal{O}_4
- ▶ Natural $\mathcal{CP}(\mathcal{O}_4)$ @ LO!!
- ▶ $\varepsilon_K - \mathcal{S}_{\psi K_S}$ anomaly removed, still SM tension for $BR(B^+ \rightarrow \tau^+ \nu)$
- ▶ Small $\delta S_{\psi\phi}$ & δA_{SI}^b experimentally allowed

Thanks!

Tools

$$\mathcal{D}_\mu \mathbf{U} \equiv \partial_\mu \mathbf{U} + \frac{ig}{2} \tau_i W_\mu^i \mathbf{U} - \frac{ig'}{2} \mathbf{U} \tau_3 B_\mu$$

$$\mathbf{T} = \mathbf{U} \tau_3 \mathbf{U}^\dagger, \quad \mathbf{T} \rightarrow L \mathbf{T} L^\dagger,$$

$$\mathbf{V}_\mu = (\mathcal{D}_\mu \mathbf{U}) \mathbf{U}^\dagger, \quad \mathbf{V}_\mu \rightarrow L \mathbf{V}_\mu L^\dagger.$$

Lagrangian for interaction between the gauge fields and the scalar sector:

$$\mathcal{L} = -\frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + \frac{v^2}{4} \text{Tr}[\mathbf{V}_\mu \mathbf{V}^\mu] + \delta\mathcal{L},$$

$$\delta\mathcal{L}_{d_X=2} = a_{WZ} \frac{v^2}{4} \text{Tr}[\mathbf{T} \mathbf{V}_\mu] \text{Tr}[\mathbf{T} \mathbf{V}^\mu],$$

Non-linear Yukawa interactions:

$$\mathcal{L}_Y = \frac{v}{\sqrt{2}} \bar{Q}_L \mathcal{Y} \mathbf{U} Q_R + \text{h.c.}, \quad Q_R = (u_R, d_R)$$

Tools

$$\mathcal{Y} \equiv \begin{pmatrix} Y_U & 0 \\ 0 & Y_D \end{pmatrix} = \begin{pmatrix} V^\dagger \mathbf{y}_U & 0 \\ 0 & \mathbf{y}_D \end{pmatrix}$$

Spurion field $\sim (8, 1, 1)$ for new FCNC effects

$$\lambda_F \equiv Y_U Y_U^\dagger + Y_D Y_D^\dagger = V^\dagger \mathbf{y}_U^2 V + \mathbf{y}_D^2$$

$d_\chi = 4$ ops.

$$\mathcal{O}_1 = \frac{i}{2} \bar{Q}_L \lambda_F \gamma^\mu \{ \mathbf{T}, \mathbf{V}_\mu \} Q_L,$$

$$\mathcal{O}_2 = i \bar{Q}_L \lambda_F \gamma^\mu \mathbf{V}_\mu Q_L,$$

$$\mathcal{O}_3 = i \bar{Q}_L \lambda_F \gamma^\mu \mathbf{T} \mathbf{V}_\mu \mathbf{T} Q_L,$$

$$\mathcal{O}_4 = \frac{1}{2} \bar{Q}_L \lambda_F \gamma^\mu [\mathbf{T}, \mathbf{V}_\mu] Q_L.$$

Effective Low-Energy Lagrangian

$$\begin{aligned} \delta \mathcal{L}_{d_\chi=4} = & -\frac{g}{\sqrt{2}} \left[W^{\mu+} \bar{U}_L \gamma_\mu (a_W + ia_{CP}) \left(\mathbf{y}_U^2 V + V \mathbf{y}_D^2 \right) D_L + h.c. \right] + \\ & -\frac{g}{2c_W} Z^\mu \left[a_Z^u \bar{U}_L \gamma_\mu \left(\mathbf{y}_U^2 + V \mathbf{y}_D^2 V^\dagger \right) U_L + a_Z^d \bar{D}_L \gamma_\mu \left(\mathbf{y}_D^2 + V^\dagger \mathbf{y}_U^2 V \right) D_L \right] \end{aligned}$$

$$a_Z^u \equiv a_1 + a_2 + a_3,$$

$$a_Z^d \equiv a_1 - a_2 - a_3,$$

$$a_W \equiv a_2 - a_3,$$

$$a_{CP} \equiv -a_4.$$

(0.1)



Non Unitarity and CP Violation

$$\tilde{V}_{ij} = V_{ij} \left[1 + (a_W + ia_{CP})(y_{u_i}^2 + y_{d_j}^2) \right]$$

$$\sum_k \tilde{V}_{ik}^* \tilde{V}_{jk} \simeq \delta_{ij} + \left[2 a_W y_t^2 + (a_W^2 + a_{CP}^2) y_t^4 \right] \delta_{it} \delta_{jt}$$

$$\sum_k \tilde{V}_{ki}^* \tilde{V}_{kj} \simeq \delta_{ij} + \left[2 a_W y_t^2 + (a_W^2 + a_{CP}^2) y_t^4 \right] V_{ti}^* V_{tj}$$

$$\begin{aligned} \arg \left(-\frac{\tilde{V}_{ik}^* \tilde{V}_{il}}{\tilde{V}_{jk}^* \tilde{V}_{jl}} \right) &= \arg \left(-\frac{V_{ik}^* V_{il}}{V_{jk}^* V_{jl}} \right) + a_{CP} \left[2 a_W (y_{u_j}^2 - y_{u_i}^2) (y_{d_l}^2 - y_{d_k}^2) + \right. \\ &\quad \left. - (3 a_W^2 - a_{CP}^2) (y_{u_j}^2 - y_{u_i}^2) (y_{d_l}^2 - y_{d_k}^2) (y_{u_i}^2 + y_{u_j}^2 + y_{d_k}^2 + y_{d_l}^2) \right] + O(a^4), \end{aligned}$$

$$\arg \left(-\frac{\tilde{V}_{tb}^* \tilde{V}_{td}}{\tilde{V}_{ub}^* \tilde{V}_{ud}} \right) \simeq \alpha + 2 y_b^2 y_t^2 a_W a_{CP},$$

$$\arg \left(-\frac{\tilde{V}_{cb}^* \tilde{V}_{cd}}{\tilde{V}_{tb}^* \tilde{V}_{td}} \right) \simeq \beta - 2 y_b^2 y_t^2 a_W a_{CP},$$

$$\arg \left(-\frac{\tilde{V}_{ub}^* \tilde{V}_{ud}}{\tilde{V}_{cb}^* \tilde{V}_{cd}} \right) \simeq \gamma - 2 y_c^2 y_b^2 a_W a_{CP} \simeq \gamma.$$

$\Delta F = 1$ observables

FCNC-effective lagrangian

$$\frac{G_F \alpha}{2\sqrt{2}\pi s_W^2} V_{ti}^* V_{tj} \sum_n C_n Q_n + \text{h.c.},$$

Wilson coefficient C_n :

$$C_n = C_n^{SM} + C_n^{NP}$$

FCNC operators basis

$$\begin{aligned}
Q_{\bar{\nu}\nu} &= \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \bar{\nu} \gamma^\mu (1 - \gamma_5) \nu, & Q_7 &= e_q \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \bar{q} \gamma^\mu (1 + \gamma_5) q, \\
Q_{9V} &= \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \bar{\ell} \gamma^\mu \ell, & Q_9 &= e_q \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \bar{q} \gamma^\mu (1 - \gamma_5) q, \\
Q_{10A} &= \bar{d}_i \gamma_\mu (1 - \gamma_5) d_j \bar{\ell} \gamma^\mu \gamma_5 \ell, & Q_{7\gamma} &= \frac{m_j}{g^2} \bar{d}_i (1 - \gamma_5) \sigma_{\mu\nu} d_j (e F^{\mu\nu}), \\
&& Q_{8G} &= \frac{m_j}{g^2} \bar{d}_i (1 - \gamma_5) \sigma_{\mu\nu} T^a d_j (g_s G_a^{\mu\nu}).
\end{aligned}$$

Leading NP contributions non-linear MFV operators:

$$\begin{aligned}
C_{\nu\bar{\nu}}^{NP} &= -\kappa y_t^2 a_Z^d, & C_7^{NP} &= +2\kappa s_W^2 y_t^2 a_Z^d, \\
C_{9V}^{NP} &= \kappa (1 - 4s_W^2) y_t^2 a_Z^d, & C_9^{NP} &= -2\kappa c_W^2 y_t^2 a_Z^d, \\
C_{10A}^{NP} &= -\kappa y_t^2 a_Z^d, & C_{7\gamma}^{NP} &= C_{8G}^{NP} = 0.
\end{aligned}$$

$B^+ \rightarrow \tau^+ \nu$

$B^+ \rightarrow \tau^+ \nu$ -tree-level charged current process.

$$BR(B^+ \rightarrow \tau^+ \nu) = \frac{G_F^2 m_{B^+} m_\tau^2}{8\pi} \left(1 - \frac{m_\tau^2}{m_{B^+}^2}\right)^2 F_{B^+}^2 |V_{ub}|^2 \left|1 + (a_W + i a_{CP}) y_b^2\right|^2 \tau_{B^+},$$

F_{B^+} is B decay constant.

$\Delta F = 1$ observables

FCNC bounds from tree level analysis

Operator	Observable	Bound (@ 95% C.L.)
\mathcal{O}_{9V}	$B \rightarrow X_s l^+ l^-$	$-0.811 < a_Z^d < 0.232$
\mathcal{O}_{10A}	$B \rightarrow X_s l^+ l^-, B \rightarrow \mu^+ \mu^-$	$-0.050 < a_Z^d < 0.009$
$\mathcal{O}_{\bar{\nu}\nu}$	$K^+ \rightarrow \pi^+ \bar{\nu}\nu$	$-0.044 < a_Z^d < 0.133$

$\Delta F = 2$ observables

$\Delta F = 2$ -effective hamiltonian

$$\mathcal{H}_{\text{eff}}^{\Delta F=2} = \frac{G_F^2 M_W^2}{4\pi^2} C(\mu) Q$$

Q neutral meson mixing operator:

$$Q = (\bar{d}_i^\alpha \gamma_\mu P_L d_j^\alpha)(\bar{d}_i^\beta \gamma^\mu P_L d_j^\beta)$$

Mixing amplitudes M_{12}^i ($i = K, d, s$):

$$M_{12}^K = \frac{\langle \bar{K}^0 | \mathcal{H}_{\text{eff}}^{\Delta S=2} | K^0 \rangle^*}{2 m_K}, \quad M_{12}^q = \frac{\langle \bar{B}_q^0 | \mathcal{H}_{\text{eff}}^{\Delta B=2} | B_q^0 \rangle^*}{2 m_{B_q}},$$

with $q = d, s$. For the K system, $M_{12}^K = (M_{12}^K)_{SM} + (M_{12}^K)_{NP}$. Neglecting all contributions proportional to $y_{u,d,s}$ and y_c^n with $n > 2$:

$$(M_{12}^K)_{SM} = R_K \left[\eta_2 \lambda_t^2 S_0(x_t) + \eta_1 \lambda_c^2 S_0(x_c) + 2 \eta_3 \lambda_t \lambda_c S_0(x_c, x_t) \right]^*,$$

$$(M_{12}^K)_{NP} = R_K \left[\eta_2 \lambda_t^2 \left(y_t^2 (2 a_W + y_t^2 a_{CP}^2) G(x_t) + \frac{(4 \pi y_t^2 a_Z^d)^2}{g^2} \right) + 2 \eta_1 \lambda_c^2 a_W y_c^2 G(x_c) \right. \\ \left. + 2 \eta_3 \lambda_t \lambda_c \left(y_t^2 (2 a_W + a_{CP}^2 y_t^2) H(x_t, x_c) + 2 a_W y_c^2 H(x_c, x_t) \right) \right]^*$$

$$R_K \equiv \frac{G_F^2 M_W^2}{12 \pi^2} F_K^2 m_K \hat{B}_K$$

$\Delta F = 2$ observables

Neutral kaon oscillation

$$\Delta M_K = 2 \left[\text{Re}(M_{12}^K)_{SM} + \text{Re}(M_{12}^K)_{NP} \right],$$
$$\varepsilon_K = \frac{\kappa_\epsilon e^{i\varphi_\epsilon}}{\sqrt{2} (\Delta M_K)_{\text{exp}}} \left[\text{Im} \left(M_{12}^K \right)_{SM} + \text{Im} \left(M_{12}^K \right)_{NP} \right]$$

Neutral meson oscillation

$$M_{12}^q = (M_{12}^q)_{SM} C_{Bq} e^{2i\varphi_{Bq}},$$

NP effects from $C_{B_{d,s}}$ and $\varphi_{B_{d,s}}$

$$M_{12}^q = R_{Bq} \left[\lambda_t^2 S_0(x_t) \right]^*, \quad \text{with} \quad R_{Bq} \equiv \frac{G_F^2 M_W^2}{12 \pi^2} F_{Bq}^2 m_{Bq} \hat{B}_{Bq} \eta_B,$$

$B_{d,s}$ -mass differences

$$\Delta M_q = 2 |M_{12}^q| \equiv (\Delta M_q)_{SM} C_{Bq},$$

$$C_{B_d} = C_{B_s} = \left| 1 + 2 a_W \left(y_t^2 \frac{G(x_t)}{S_0(x_t)} + y_b^2 \right) + \frac{(4 \pi y_t^2 a_Z^d)^2}{g^2 S_0(x_t)} + 2 i a_W a_{CP} y_t^2 y_b^2 \frac{G(x_t)}{S_0(x_t)} \right|.$$

$\Delta F = 2$ observables

Neutral meson oscillation

Mixing-induced CP asymmetries $S_{\psi K_S}$ & $S_{\psi\phi}$ for $B_d^0 \rightarrow \psi K_S$ & $B_s^0 \rightarrow \psi\phi$

$$S_{\psi K_S} = \sin(2\beta + 2\varphi_{B_d}), \quad S_{\psi\phi} = \sin(2\beta_s - 2\varphi_{B_s}),$$

UT-angles β & β_s

$$\beta \equiv \arg\left(-\frac{V_{cb}^* V_{cd}}{V_{tb}^* V_{td}}\right), \quad \beta_s \equiv \arg\left(-\frac{V_{tb}^* V_{ts}}{V_{cb}^* V_{cs}}\right),$$

New phases

$$\varphi_{B_d} = \varphi_{B_s} = 2 a_W a_{CP} y_t^2 y_b^2 \frac{G(x_t)}{S_0(x_t)}.$$

$R_{BR/\Delta M}$

$$R_{BR/\Delta M} = \frac{3\pi\tau_{B^+}}{4\eta_B \hat{B}_{B_d} S_0(x_t)} \frac{m_\tau^2}{M_W^2} \frac{|V_{ub}|^2}{|V_{tb}^* V_{td}|^2} \left(1 - \frac{m_\tau^2}{m_{B_d}^2}\right)^2 \frac{|1 + (a_W + i a_{CP}) y_b^2|^2}{C_{B_d}}$$

$\Delta F = 2$ observables

B-semileptonic CP-Asymmetry

$$A_{sl}^b \equiv \frac{N_b^{++} - N_b^{--}}{N_b^{++} + N_b^{--}},$$

N_b^{++} & N_b^{--} number of events containing two μ^+ or μ^- . In $p\bar{p}$ colliders, such events can only arise through $B_d^0 - \bar{B}_d^0$ or $B_s^0 - \bar{B}_s^0$ mixings.

$$A_{sl}^b = (0.594 \pm 0.022) a_{sl}^d + (0.406 \pm 0.022) a_{sl}^s,$$

$$a_{sl}^d \equiv \left| \frac{(\Gamma_{12}^d)_{SM}}{(M_{12}^d)_{SM}} \right| \sin \phi_d = (5.4 \pm 1.0) \times 10^{-3} \sin \phi_d,$$

$$a_{sl}^s \equiv \left| \frac{(\Gamma_{12}^s)_{SM}}{(M_{12}^s)_{SM}} \right| \sin \phi_s = (5.0 \pm 1.1) \times 10^{-3} \sin \phi_s,$$

$$\phi_d \equiv \arg \left(- (M_{12}^d)_{SM} / (\Gamma_{12}^d)_{SM} \right) = -4.3^\circ \pm 1.4^\circ,$$

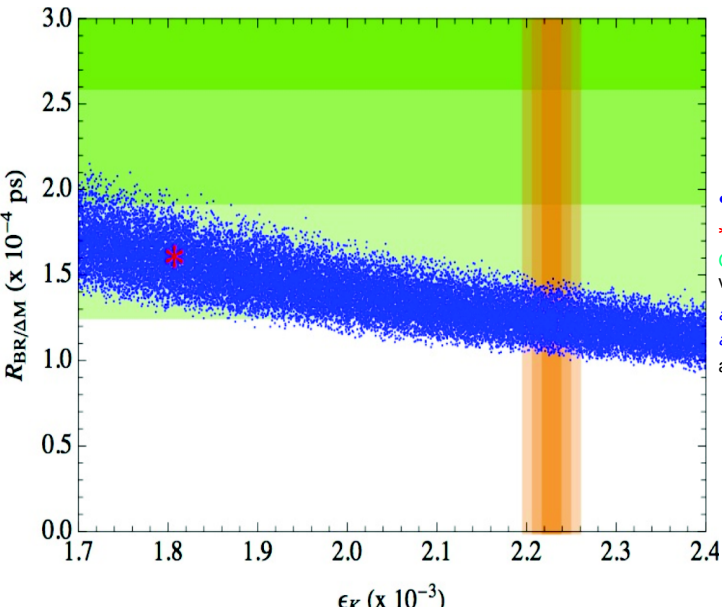
$$\phi_s \equiv \arg \left(- (M_{12}^s)_{SM} / (\Gamma_{12}^s)_{SM} \right) = 0.22^\circ \pm 0.06^\circ.$$

NP contributions

$$\Gamma_{12}^q = (\Gamma_{12}^q)_{SM} \tilde{C}_{Bq} \quad \text{with} \quad \tilde{C}_{Bq} = 1 + 2 a_W y_b^2,$$

$$a_{sl}^q = \left| \frac{(\Gamma_{12}^q)_{SM}}{(M_{12}^q)_{SM}} \right| \frac{\tilde{C}_{Bq}}{C_{Bq}} \sin \left(\phi_q + 2\varphi_{Bq} \right),$$

ϵ_K vs. $R_{BR/\Delta M}$ from $\mathcal{O}_{1,2,3}$



- : correlation $\epsilon_K - R_{BR/\Delta M}$
- *: SM values
- Green & Orange: 1, 2, 3 σ exp values
- $a_W \in [-1, 1]$,
- $a_Z^d \in [-0.1, 0.1]$
- and $a_{CP} = 0$

Phenomenological Analysis

Input parameters and the SM analysis

- ▶ Wolfenstein parametrization to describe the CKM matrix, where the parameters are fixed considering the value of V_{us} , V_{cb} , γ and $|V_{ub}|$, which are related to tree-level processes and therefore hardly affected by NP contributions.
- ▶ V_{us} and V_{cb} appear to be relatively well measured, compared to V_{ub} which has an error still of the order of 10%.
- ▶ Actual tension between the exclusive and the inclusive experimental determinations of $|V_{ub}|$, which translates into the well known $\varepsilon_K - S_{\psi K_S}$ and $BR(B^+ \rightarrow \tau^+ \nu)$ anomalies.
- ▶ γ of the B_d unitarity triangle, despite of being a tree-level SM processes, still suffers from a large uncertainty. Two scenarios:
- ▶ **Exclusive determination** of $|V_{ub}|$, $S_{\psi K_S}$ is predicted to be very close to the experimental determination of $\sin(2\beta)_{b \rightarrow c\bar{c}s}$, while $\varepsilon_K \approx 1.8 \times 10^{-3}$ is clearly below the measured value. Furthermore, for such a value of $|V_{ub}|$ the $BR(B^+ \rightarrow \tau^+ \nu)$ is predicted to be smaller than the central experimental value by more than 2σ . **If NP is advocated in order to solve (or at least to soften) these anomalies it should enhance the value of ε_K and $BR(B^+ \rightarrow \tau^+ \nu)$, while having negligible impact on $S_{\psi K_S}$.**
- ▶ **Inclusive determination** of $|V_{ub}|$, the SM prediction for ε_K is closer to its experimental determination and $BR(B^+ \rightarrow \tau^+ \nu)$ agrees with exp. within the 1σ level. However, $S_{\psi K_S}$ is above the measured value. **If NP is advocated in order to solve (or at least to soften) this anomaly, it should deplete $S_{\psi K_S}$, while leaving basically unchanged ε_K and $BR(B^+ \rightarrow \tau^+ \nu)$.**

Phenomenological Analysis

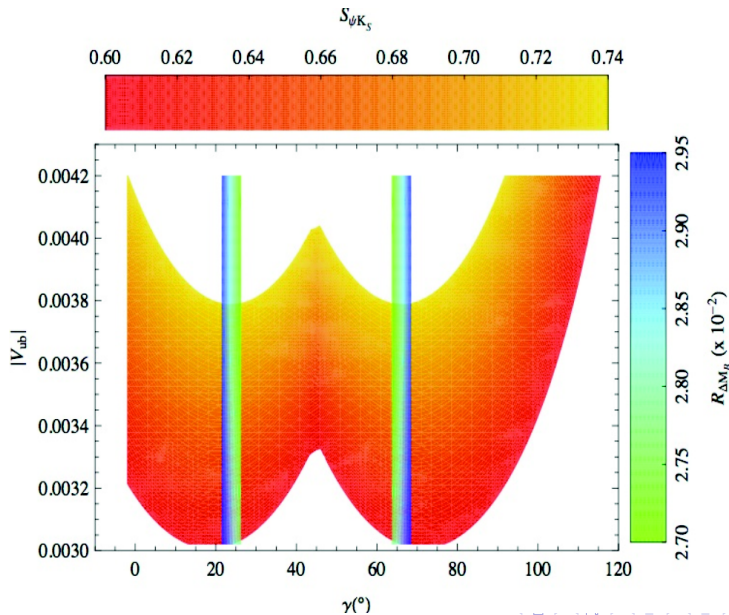
Input parameters and the SM analysis

$G_F = 1.16637(1) \times 10^{-5} \text{ GeV}^{-2}$	[30]	$m_{B_d} = 5279.5(3) \text{ MeV}$	[30]
$M_W = 80.399(23) \text{ GeV}$	[30]	$m_{B_s} = 5366.3(6) \text{ MeV}$	[30]
$s_W^2 \equiv \sin^2 \theta_W = 0.23116(13)$	[30]	$F_{B_d} = 205(12) \text{ MeV}$	[32]
$\alpha(M_Z) = 1/127.9$	[30]	$F_{B_s} = 250(12) \text{ MeV}$	[32]
$\alpha_s(M_Z) = 0.1184(7)$	[30]	$\hat{B}_{B_d} = 1.26(11)$	[32]
$m_u(2 \text{ GeV}) = 1.7 \div 3.1 \text{ MeV}$	[30]	$\hat{B}_{B_s} = 1.33(6)$	[32]
$m_d(2 \text{ GeV}) = 4.1 \div 5.7 \text{ MeV}$	[30]	$F_{B_d} \sqrt{\hat{B}_{B_d}} = 233(14) \text{ MeV}$	[32]
$m_s(2 \text{ GeV}) = 100^{+30}_{-20} \text{ MeV}$	[30]	$F_{B_s} \sqrt{\hat{B}_{B_s}} = 288(15) \text{ MeV}$	[32]
$m_c(m_c) = (1.279 \pm 0.013) \text{ GeV}$	[36]	$\xi = 1.237(32)$	[32]
$m_b(m_b) = 4.19^{+0.18}_{-0.06} \text{ GeV}$	[30]	$\eta_B = 0.55(1)$	[37, 38]
$M_t = 172.9 \pm 0.6 \pm 0.9 \text{ GeV}$	[30]	$\Delta M_d = 0.507(4) \text{ ps}^{-1}$	[30]
$m_K = 497.614(24) \text{ MeV}$	[30]	$\Delta M_s = 17.77(12) \text{ ps}^{-1}$	[30]
$F_K = 156.0(11) \text{ MeV}$	[32]	$\sin(2\beta)_{b \rightarrow c\bar{c}s} = 0.673(23)$	[30]
$\hat{B}_K = 0.737(20)$	[32]	$\phi_s^{\psi\phi} = 0.55^{+0.38}_{-0.36}$	[39, 40]
$\kappa_\epsilon = 0.923(6)$	[41]	$\phi_s^{\psi\phi} = 0.03 \pm 0.16 \pm 0.07$	[42]
$\varphi_\epsilon = (43.51 \pm 0.05)^\circ$	[43]	$R_{\Delta M_B} = (2.85 \pm 0.03) \times 10^{-2}$	[30]
$\eta_1 = 1.87(76)$	[44]	$A_{sl}^b = (-0.787 \pm 0.172 \pm 0.093) \times 10^{-2}$	[34]
$\eta_2 = 0.5765(65)$	[37]	$ V_{us} = 0.2252(9)$	[30]
$\eta_3 = 0.496(47)$	[45]	$ V_{cb} = (40.6 \pm 1.3) \times 10^{-3}$	[30]
$\Delta M_K = 0.5292(9) \times 10^{-2} \text{ ps}^{-1}$	[30]	$ V_{ub}^{\text{incl.}} = (4.27 \pm 0.38) \times 10^{-3}$	[30]
$ \epsilon_K = 2.228(11) \times 10^{-3}$	[30]	$ V_{ub}^{\text{excl.}} = (3.38 \pm 0.36) \times 10^{-3}$	[30]
$\tau_{B^\pm} = (1641 \pm 8) \times 10^{-3} \text{ ps}$	[30]	$ V_{ub}^{\text{comb.}} = (3.89 \pm 0.44) \times 10^{-3}$	[30]
$BR(B^+ \rightarrow \tau^+ \nu) = (1.65 \pm 0.34) \times 10^{-4}$	[30]	$\gamma = (73^{+22}_{-25})^\circ$	[30]

Table 2: Values of the experimental quantities used as input parameters. Notice that $m_i(m_i)$ are the masses m_i at the scale m_i in the \overline{MS} scheme while M_t is the top-quark pole mass.

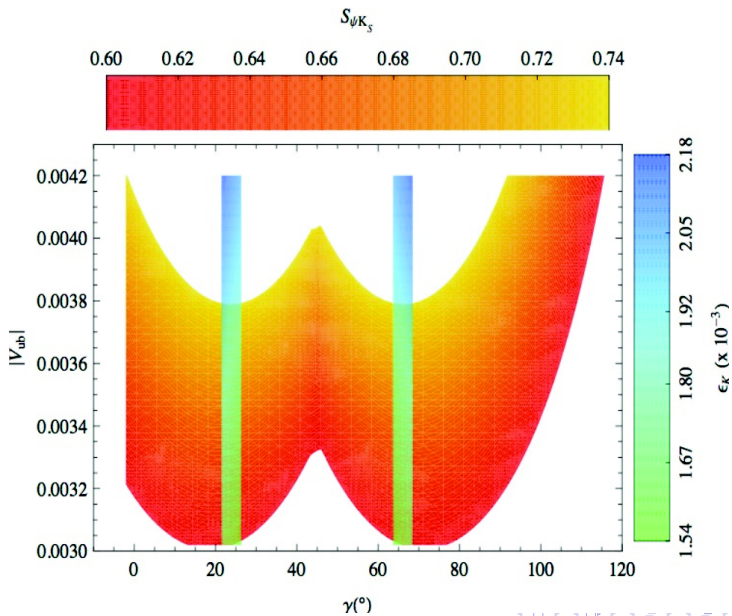
Phenomenological Analysis

$|V_{ub}| - \gamma$ parameter space



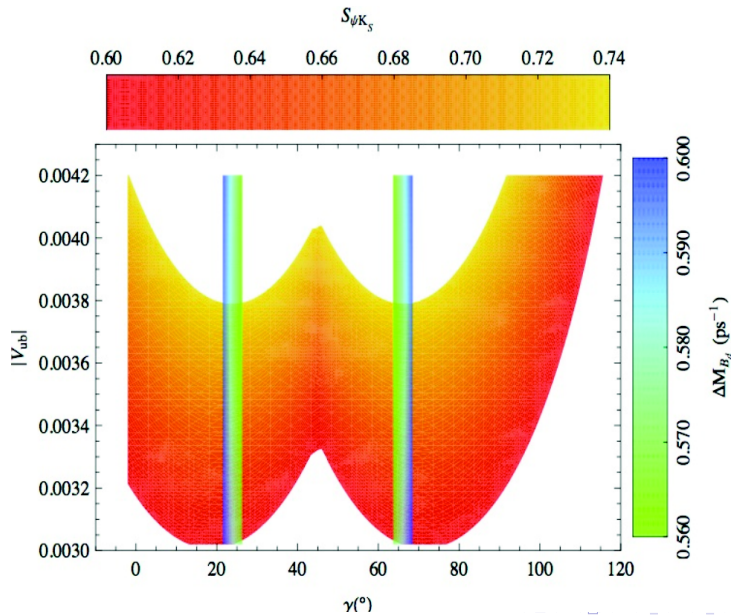
Phenomenological Analysis

ϵ_K



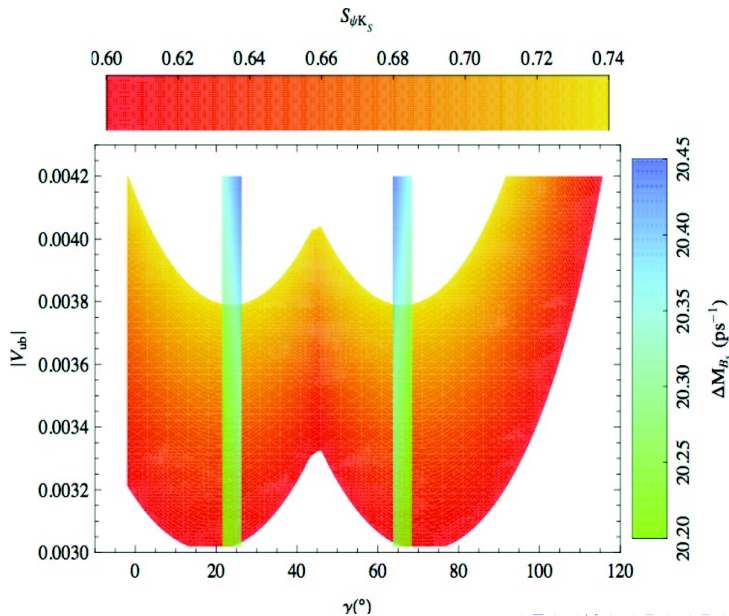
Phenomenological Analysis

$$\Delta M_{B_d}$$



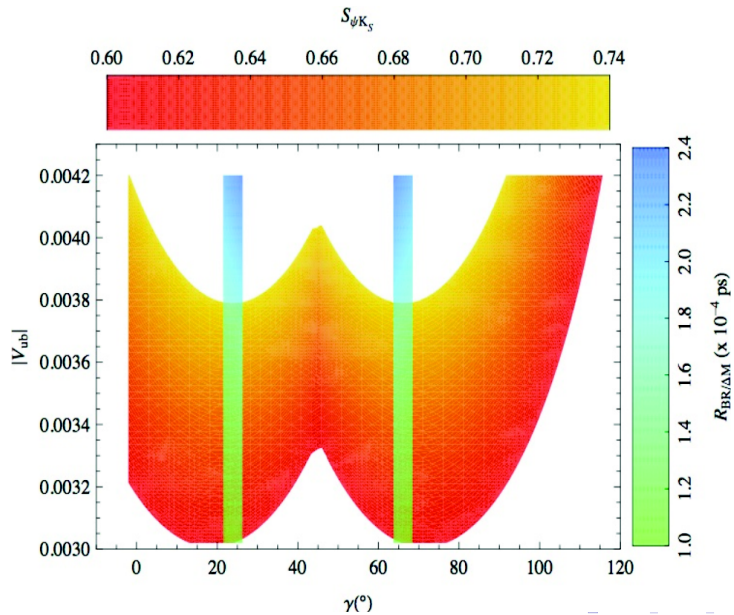
Phenomenological Analysis

$$\Delta M_{B_s}$$



Phenomenological Analysis

$$R_{BR/\Delta M}$$



Phenomenological Analysis

In order to illustrate the features of the MFV scenario with a strong interacting Higgs sector, the numerical analysis of the following sections will be presented choosing as reference point, $(|V_{ub}|, \gamma) = (3.5 \times 10^{-3}, 66^\circ)$, corresponding to $S_{\psi K_S} \simeq 0.692$ and $R_{\Delta M_B} \simeq 2.83 \times 10^{-2}$. For this point

$$\varepsilon_K = 1.8 \times 10^{-3}, \quad R_{BR/\Delta M} = 1.6 \times 10^{-4} \text{ ps}.$$

$$S_{\psi\phi} = 0.036.$$

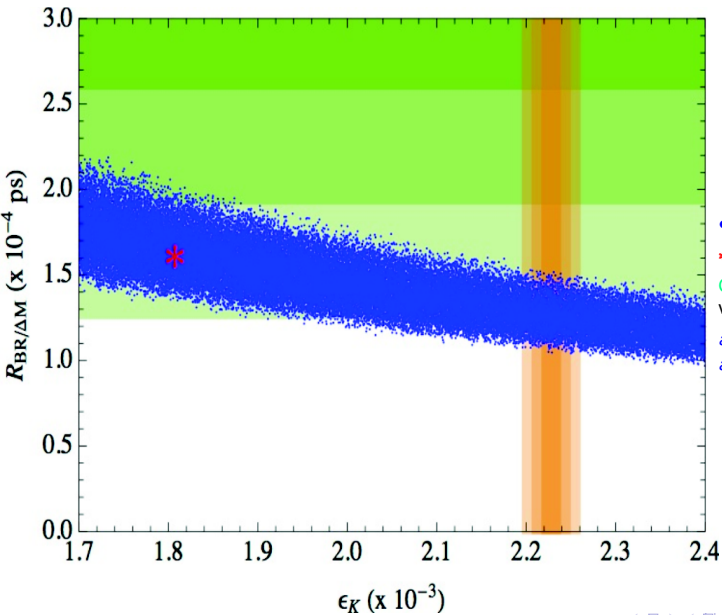
$$A_{sl}^b = -2.3 \times 10^{-4} \quad \left(a_{sl}^d = -4.0 \times 10^{-4}, \quad a_{sl}^s = 1.9 \times 10^{-5} \right),$$

$$a_{CP} = 0.1(-0.1) \quad \longrightarrow \quad \delta A_{sl}^b \approx 1.1\%(1.6\%)$$

$$a_W = 0.1(-0.1) \quad \longrightarrow \quad \delta A_{sl}^b \approx 33\%(-23\%)$$

$$a_Z^d = \pm 0.1 \quad \longrightarrow \quad \delta A_{sl}^b \approx 160\%.$$

ϵ_K vs. $R_{BR/\Delta M}$ from all O_i



•: correlation $\epsilon_K - R_{BR/\Delta M}$

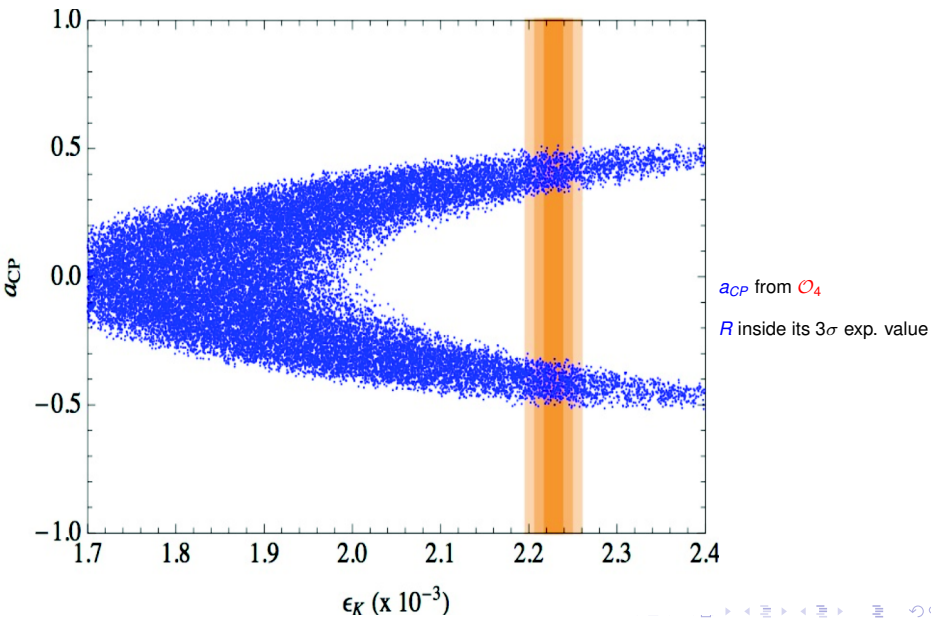
*: SM values

Green & Orange: 1, 2, 3 σ exp values

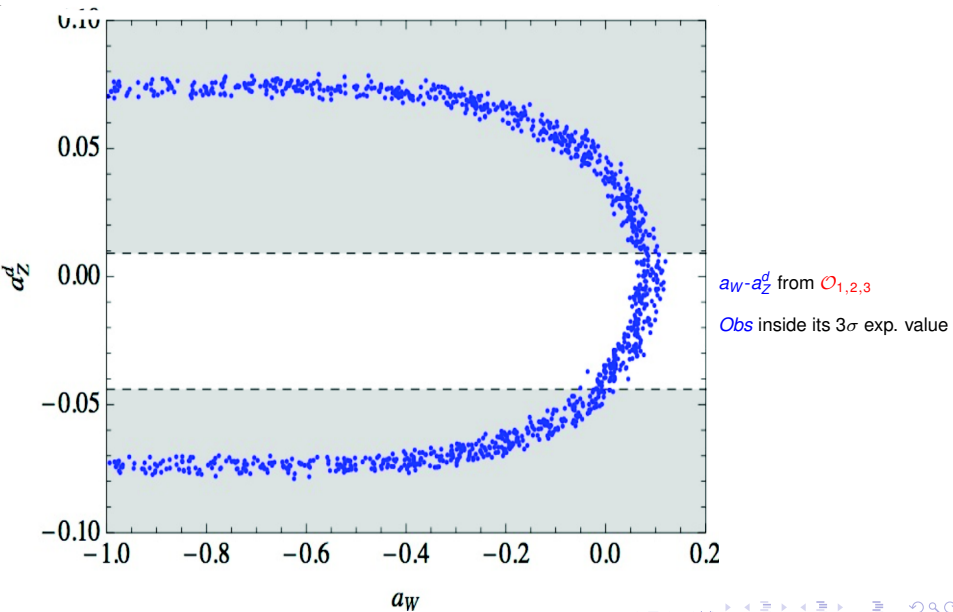
$a_W, a_{CP} \in [-1, 1]$,

$a_Z^d \in [-0.1, 0.1]$

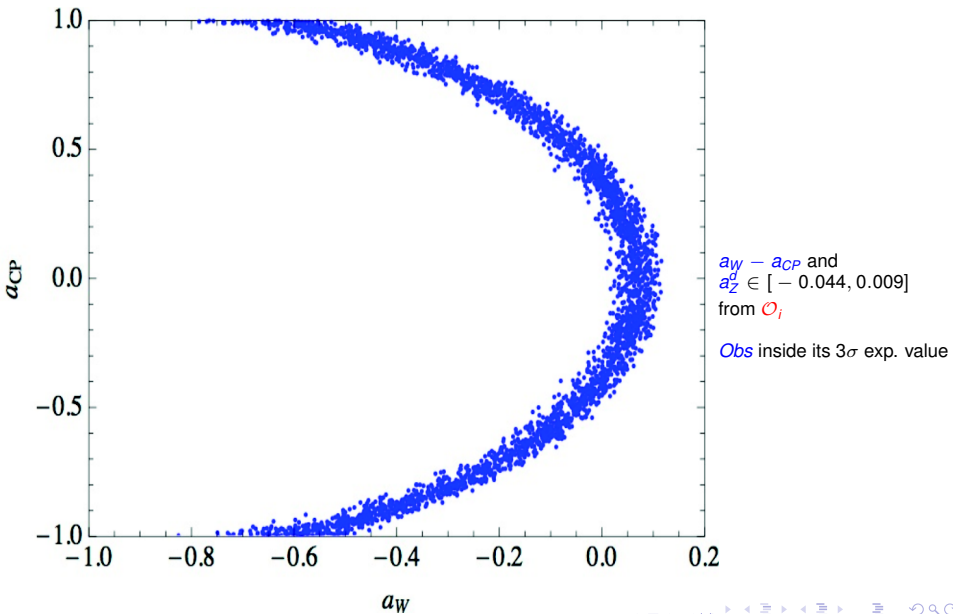
From \mathcal{O}_4



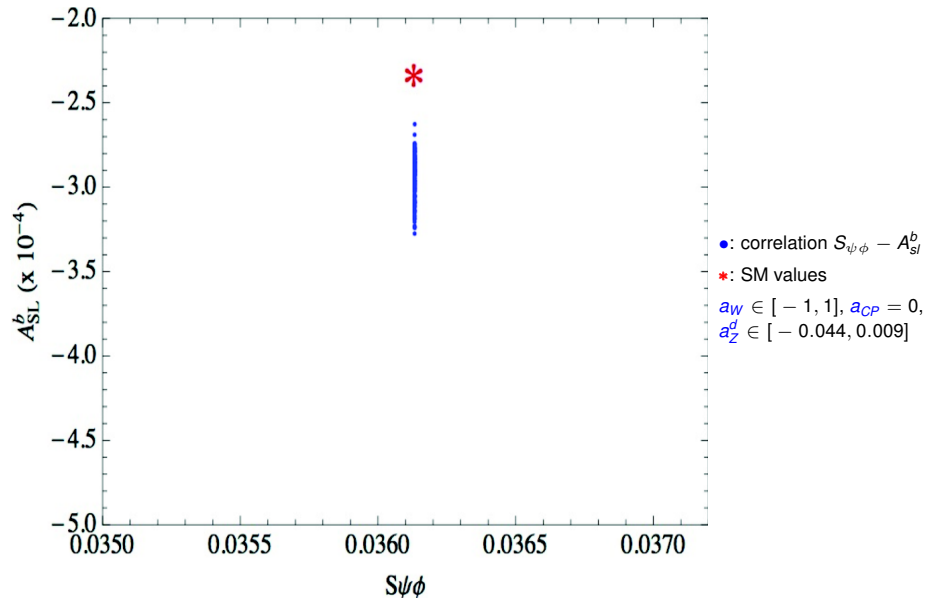
From $\mathcal{O}_{1,2,3}$



From all \mathcal{O}_i



$S_{\psi\phi}$ vs. A_{sl}^b from $\mathcal{O}_{1,2,3}$



$S_{\psi\phi}$ vs. A_{sl}^b from all \mathcal{O}_i

