

Non-unitarity & Non-standard Interactions (NSIs)

- ⇒ Part 1: Non-unitarity (theory) – S. A.
- ⇒ Part 2: Non-unitarity (bounds) – Mattias Blennow
- ⇒ Part 3: NSIs (theory) – Enrique Fernandez-Martinez
- ⇒ Part 4: NSIs (bounds) – Toshihiko Ota

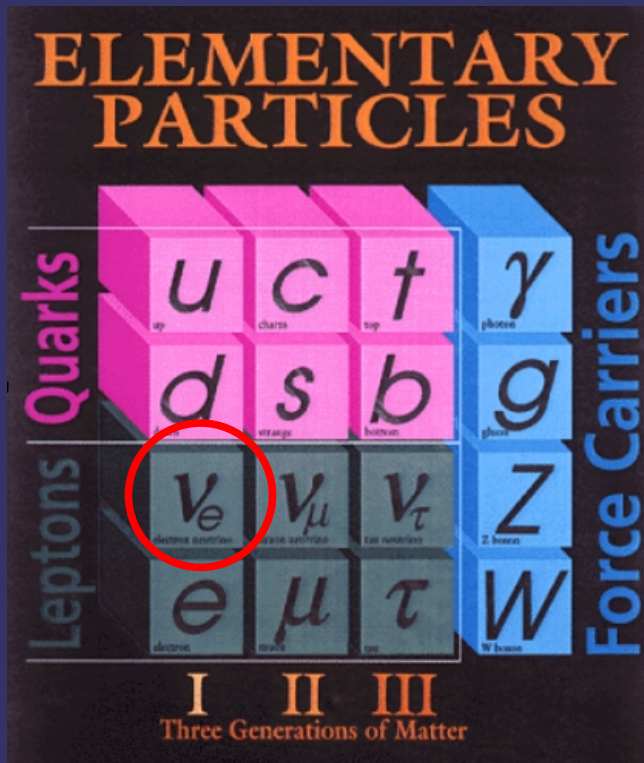


Overview

- ➔ Origin of Non-Unitarity; minimal scheme (MUV)
- ➔ Recent study: Non-unitarity of U_{PMNS} and leptogenesis?



Neutrinos in the Standard Model



⇒ Symmetries of the SM:

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$

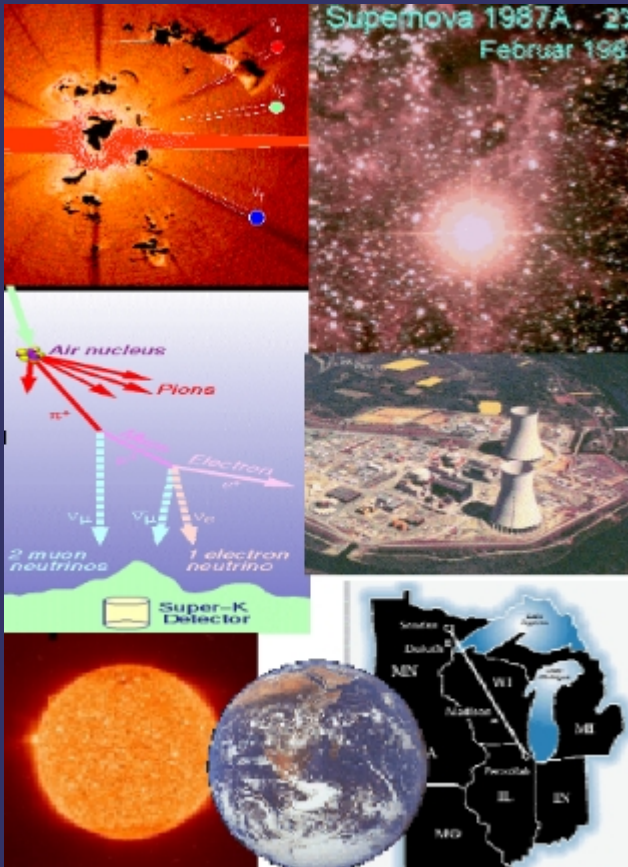
$$\begin{array}{c} \langle H \rangle = v \\ \longrightarrow \end{array} \begin{array}{c} \text{EW} \\ SU(3)_C \times U(1)_{em} \end{array}$$

⇒ Masses of elementary particles via the Higgs mechanism (exception: neutrinos remain massless)

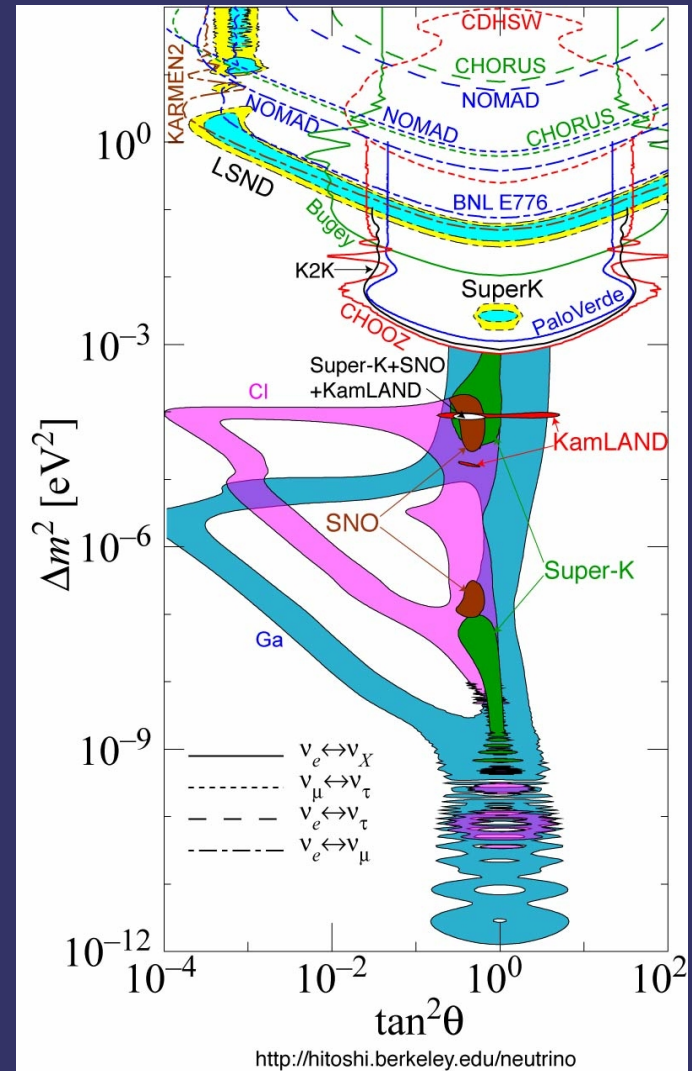
- With symmetries and field content of the SM:
 - neutrinos are massless
 - no mixing
 - couple only to Z and W (in standard way)



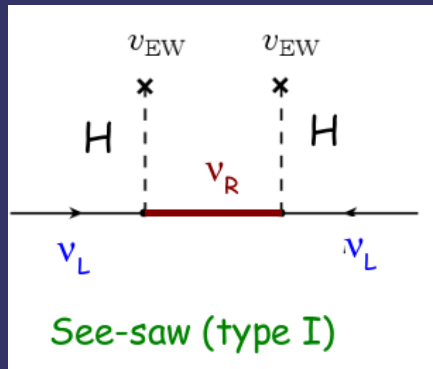
However: Evidence for ν masses!



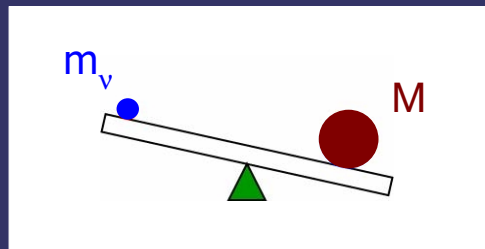
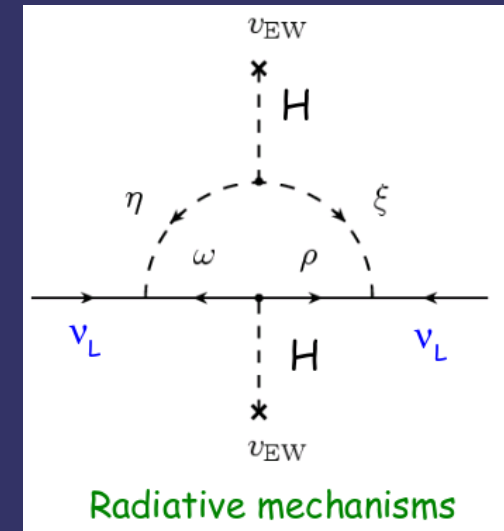
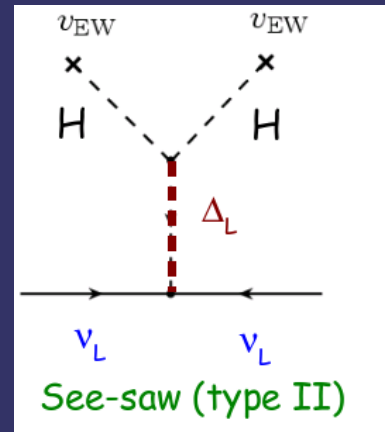
- Strong evidence for ν -oscillations:
 - ⇒ Neutrinos have mass
 - leptonic mixing matrix
 - new ν -interactions (mechanism of mass generation)



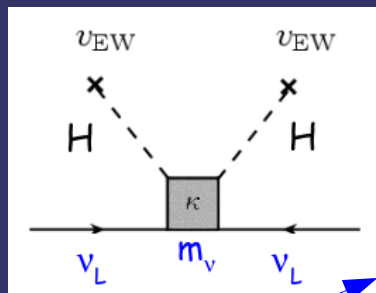
Origin of neutrino masses?



(or type III)



Smallness of m_ν : Seesaw mechanism?



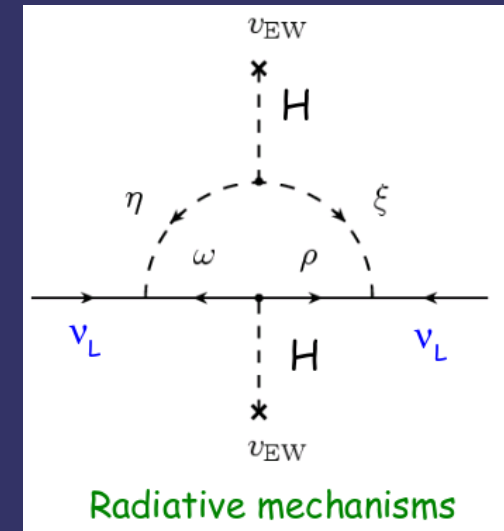
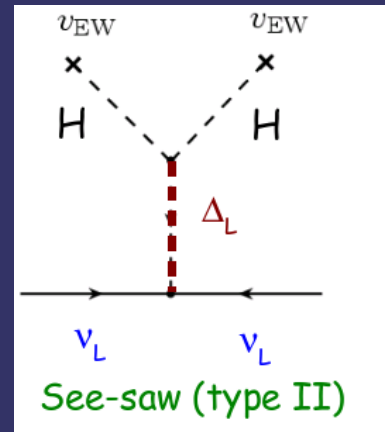
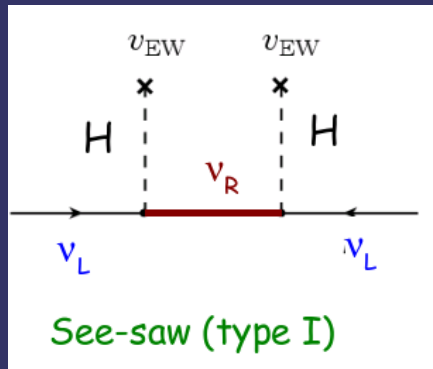
quite model independent:
unique dim. 5 Operator

$$\delta\mathcal{L}^{d=5} = \frac{1}{2} c_{\alpha\beta}^{d=5} \left(\overline{L^c}_\alpha \tilde{\phi}^* \right) \left(\tilde{\phi}^\dagger L_\beta \right) + h.c.$$

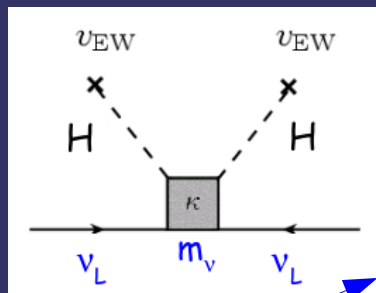
P. Minkowski ('77), Mohapatra, Senjanovic, Yanagida, Gell-Mann, Ramond, Slansky, Schechter, Valle, Magg, Wetterich, Ma, Foot, Lew, He, Joshi, ...



Origin of neutrino masses?



Smallness of m_ν :
 ... or because lepton number symmetry is violated only by small amount?



quite model independent:
 unique dim. 5 Operator

Example: so-called 'Inverse seesaw'

$$M_\nu = \begin{pmatrix} 0 & D_N^T & 0 \\ D_N & 0 & X_N^T \\ 0 & X_N & \mu \end{pmatrix}$$

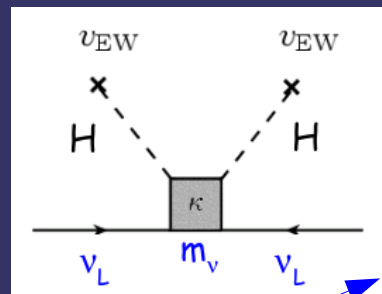
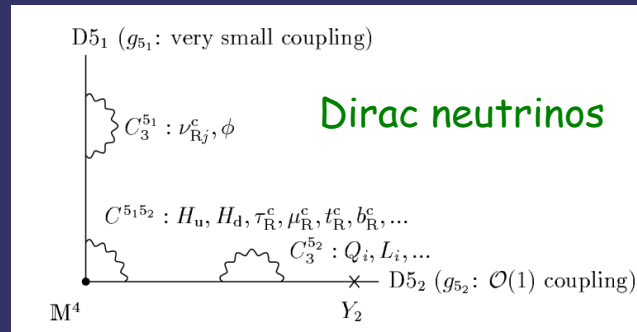
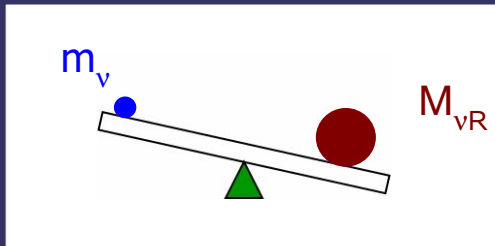
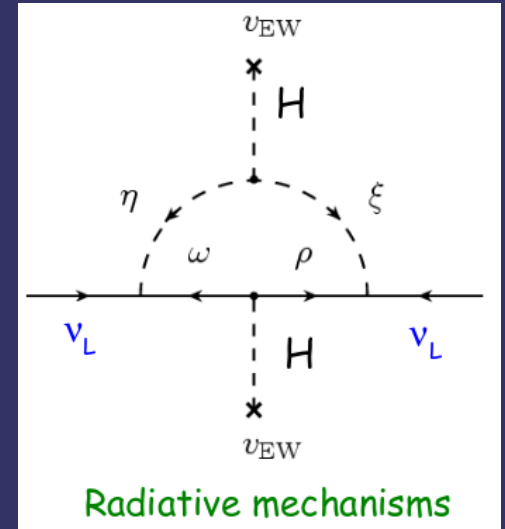
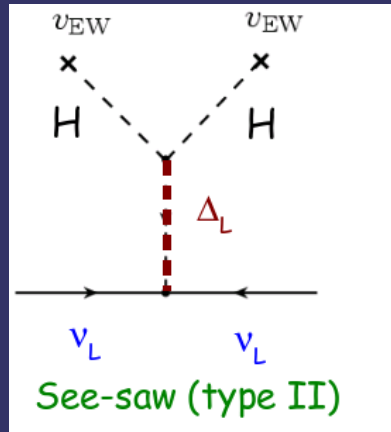
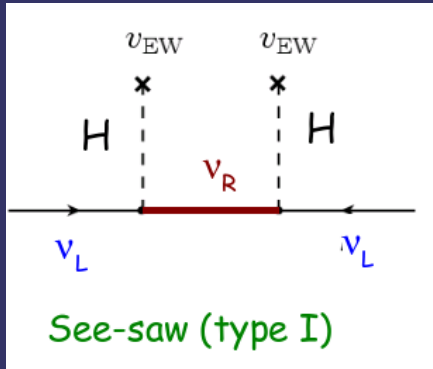
small

Mohapatra, Valle ('86)

$$\delta\mathcal{L}^{d=5} = \frac{1}{2} c_{\alpha\beta}^{d=5} \left(\overline{L^c}_\alpha \tilde{\phi}^* \right) \left(\tilde{\phi}^\dagger L_\beta \right) + h.c.$$

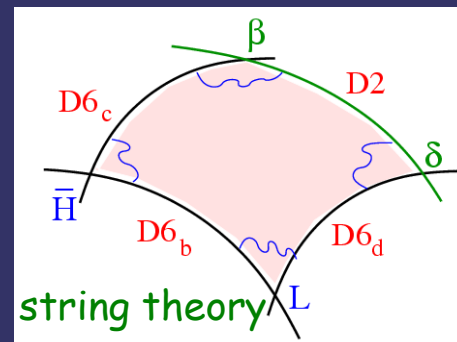
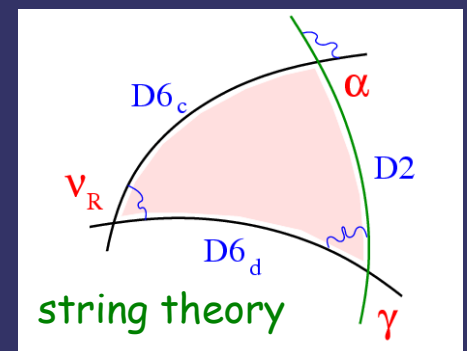


Origin of neutrino masses?



quite model independent:
unique dim. 5 Operator

$$\delta \mathcal{L}^{d=5} = \frac{1}{2} c_{\alpha\beta}^{d=5} \left(\bar{L}^c_{\alpha} \tilde{\phi}^* \right) \left(\tilde{\phi}^{\dagger} L_{\beta} \right) + h.c.$$



- Unknown:**
- which mechanism?
 - at which scale?
 - which new interactions (effects beyond m_{ν})?

Status: Neutrino masses & mixing

⇒ Known:

- (At least) two of the light neutrinos are massive
- Large mixing

⇒ Unknown:

- Which mechanism generates the neutrino masses? Dirac or Majorana?
- At which scale?
- Which additional interactions are generated (effects beyond ν -masses)
→ chance to distinguish ν -mass mechanisms

Since new interactions in the lepton sector are required (to generate ν -masses):

Is the (effective low energy) leptonic mixing matrix unitary?

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

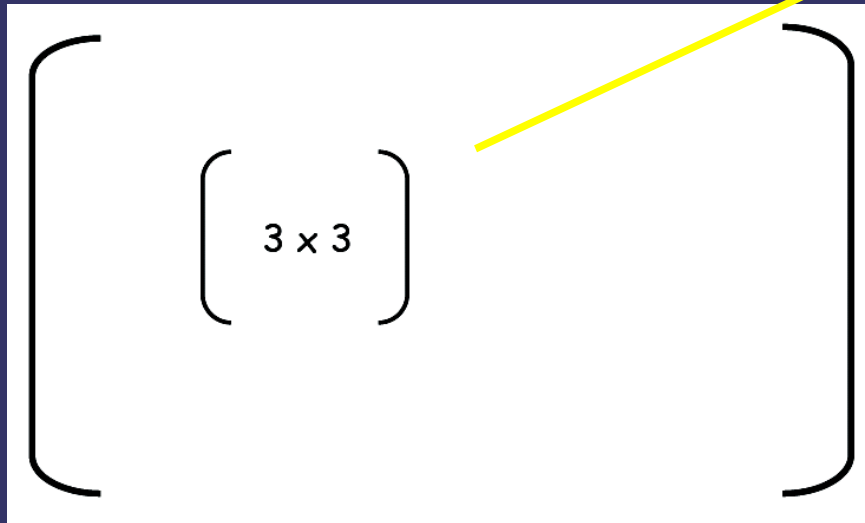
$$U U^\dagger = 1?$$

Non-unitarity (theory)



Origin of Non-Unitarity in Extensions of the SM

- ➔ Typical situation, intuitively:



(Effective) mixing matrix of light neutrinos is part of a larger unitary mixing matrix (mixing with additional heavy particles)

⇒ U_{PMNS} **non-unitary**

Examples with possible large non-unitarity: 'inverse' seesaw or 'multiple' seesaw at TeV energies, SUSY with R-parity violation, large extra dimensions, ...



Non-unitary leptonic mixing

⇒ Lagrangian in the mass basis ...

kin. term

ν -mass term

charged current interaction

non-unitary
matrix N

$$\mathcal{L}^{eff} = \frac{1}{2} (\bar{\nu}_i i \not{\partial} \nu_i - \bar{\nu}^c_i m_i \nu_i + h.c.) - \frac{g}{2\sqrt{2}} (W_\mu^+ \bar{l}_\alpha \gamma_\mu (1 - \gamma_5) N_{\alpha i} \nu_i + h.c.) \\ - \frac{g}{2 \cos \theta_W} (Z_\mu \bar{\nu}_i \gamma^\mu (1 - \gamma_5) (N^\dagger N)_{ij} \nu_j + h.c.) + \dots$$

modification in neutral current interaction:
will be justified later ...



... now we change to the flavour basis

- ➔ Field transformation: $\nu_\alpha = N_{\alpha i} \nu_i$

non-canonical kin. terms

$$\begin{aligned} \mathcal{L}^{eff} = & \frac{1}{2} \left(i \bar{\nu}_\alpha \not{\partial} (NN^\dagger)^{-1}_{\alpha\beta} \nu_\beta - \bar{\nu}^c_\alpha [(N^{-1})^t m N^{-1}]_{\alpha\beta} \nu_\beta + h.c. \right) \\ & - \frac{g}{2\sqrt{2}} \left(W_\mu^+ \bar{l}_\alpha \gamma^\mu (1 - \gamma_5) \nu_\alpha + h.c. \right) \\ & - \frac{g}{2 \cos \theta_W} \left(Z_\mu \bar{\nu}_\alpha \gamma^\mu (1 - \gamma_5) \nu_\alpha + h.c. \right) + \dots, \end{aligned}$$

Non-unitary
leptonic mixing



Non-canonical
kinetic term



Non-unitary leptonic mixing

Gauge invariant non-canonical kinetic term in the SM: e.g.

$$\delta\mathcal{L}^{d=6} = c_{\alpha\beta}^{d=6} \left(\bar{L}_\alpha \tilde{\phi} \right) i\cancel{\partial} \left(\tilde{\phi}^\dagger L_\beta \right)$$

unique dim. 6 operator leading to
non-can. kinetic terms for neutrinos only
conserves L!

Effects after EW symmetry
breaking (in mass basis):

non-unitary
matrix N

$$\begin{aligned} \mathcal{L}^{eff} = & \frac{1}{2} (\bar{\nu}_i i \cancel{\partial} \nu_i - \bar{\nu}_i^c m_i \nu_i + h.c.) - \frac{g}{2\sqrt{2}} (W_\mu^+ \bar{l}_\alpha \gamma_\mu (1 - \gamma_5) N_{\alpha i} \nu_i + h.c.) \\ & - \frac{g}{2 \cos \theta_W} (Z_\mu \bar{\nu}_i \gamma^\mu (1 - \gamma_5) (N^\dagger N)_{ij} \nu_j + h.c.) + \dots \end{aligned}$$

in addition: modification in neutral current interaction



Non-unitary leptonic mixing

- ➔ Which neutrino mass mechanisms (or other SM extensions) lead to non-unitary leptonic mixing?



Non-unitarity and neutrino masses from heavy fermionic singlets

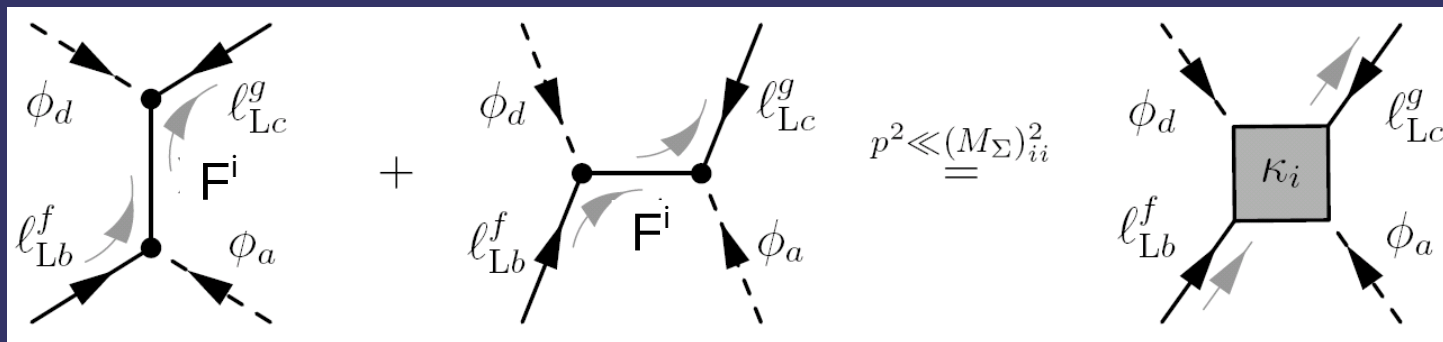
- ➔ Consider the SM + 'heavy' singlet fermions F^i as effective field theory:
 - 'heavy' = large mass compared to the energies of the experiment
 - effective theory: below the masses of the singlet fermions



Non-unitarity and **neutrino masses** from heavy fermionic singlets

- ⇒ Consider the SM + 'heavy' singlet fermions F^i as effective field theory:
 - 'heavy' = large mass compared to the energies of the experiment
 - effective theory: below the masses of the singlet fermions

- ⇒ At **dimension 5 operator** level:



violates L!



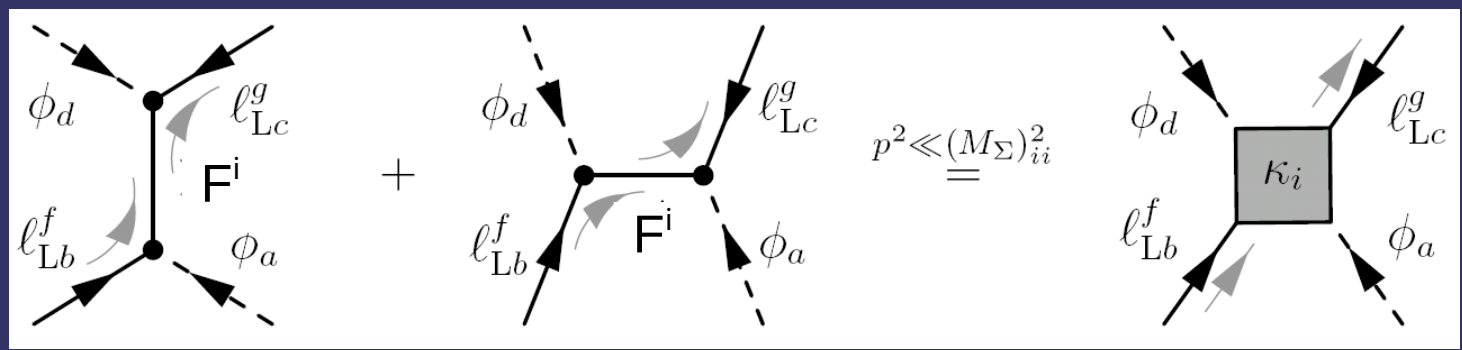
Non-unitarity and **neutrino masses** from heavy fermionic singlets

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Weinberg ('79)

$$\delta\mathcal{L}^{d=5} = \frac{1}{2} c_{\alpha\beta}^{d=5} \left(\overline{L^c_\alpha} \tilde{\phi}^* \right) \left(\tilde{\phi}^\dagger L_\beta \right) + h.c.$$

- ➔ At **dimension 5 operator** level:



violates L!

After EW symmetry breaking:

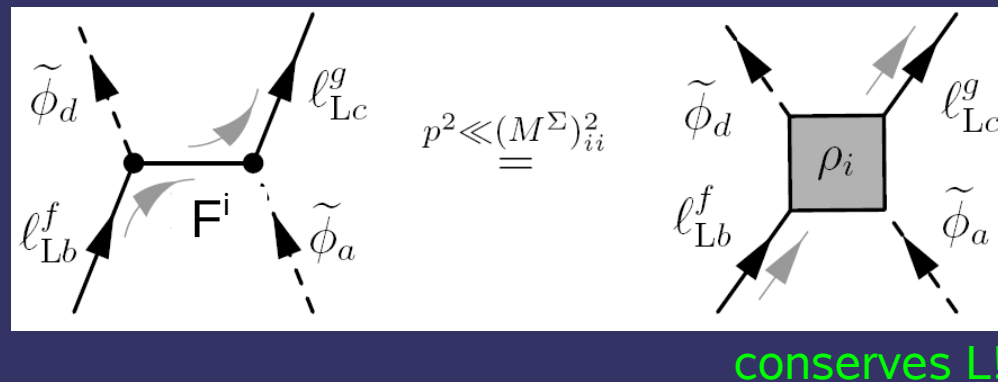
$$m_\nu \equiv -\frac{v^2}{2} c^{d=5}$$

Seesaw (type I)



Non-unitarity and neutrino masses from heavy fermionic singlets

- ⇒ Consider the SM + 'heavy' singlet fermions F^i as effective field theory:
 - 'heavy' = large mass compared to the energies of the experiment
 - effective theory: below the masses of the singlet fermions
- ⇒ At **dimension 6 operator** level:

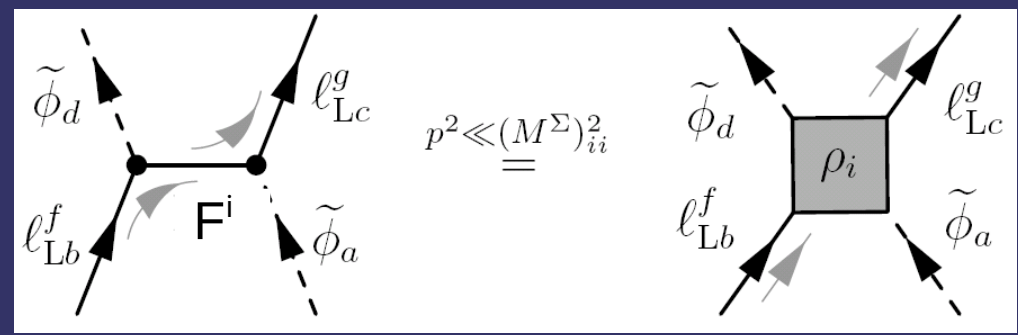


Non-unitarity and neutrino masses from heavy fermionic singlets

- Consider the SM + 'heavy' singlet fermions F^i as effective field theory:
 - 'heavy' = large mass compared to the energies of the experiment
 - effective theory: below the masses of the singlet fermions

→ At dimension 6 operator level:

$$\delta\mathcal{L}^{d=6} = c_{\alpha\beta}^{d=6} \left(\bar{L}_\alpha \tilde{\phi} \right) i \not{\partial} \left(\tilde{\phi}^\dagger L_\beta \right)$$



conserves L!

De Gouvea, Giudice, Strumia, Tobe ('01)
Broncano, Gavela Jenkins ('02)

After EW symmetry breaking: Non-unitarity

$$|NN^\dagger - 1|_{\alpha\beta} = \frac{v^2}{2} |c^{d=6}|_{\alpha\beta}$$

via non-canonical kin. terms for neutrinos!

S.A., Biggio, Fernandez-Martinez, Gavela, Lopez-Pavon ('06)

Stefan Antusch
MPI für Physik (Munich)



Effective theory extension of SM: Minimal unitarity violation (MUV)

S.A., Biggio, Fernandez-Martinez,
Gavela, Lopez-Pavon ('06)

$$\mathcal{L}^{eff} = \mathcal{L}_{SM} + \delta\mathcal{L}^{d=5} + \delta\mathcal{L}^{d=6} + \dots$$

where

$$\delta\mathcal{L}^{d=5} = \frac{1}{2} c_{\alpha\beta}^{d=5} \left(\bar{L}_\alpha^c \tilde{\phi}^* \right) \left(\tilde{\phi}^\dagger L_\beta \right) + h.c.$$

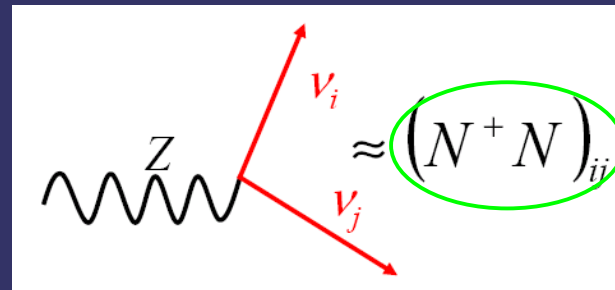
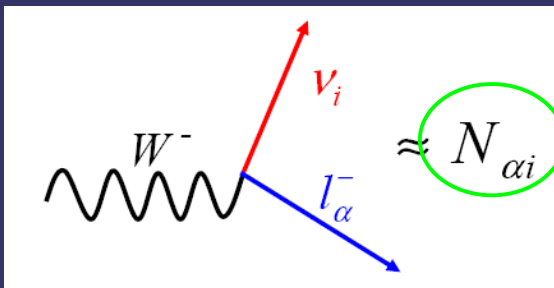
unique dim. 5 operator for
neutrino masses **violates L!**

$$\delta\mathcal{L}^{d=6} = c_{\alpha\beta}^{d=6} \left(\bar{L}_\alpha \tilde{\phi} \right) i \not{\partial} \left(\tilde{\phi}^\dagger L_\beta \right)$$

unique dim. 6 operator leading to
non-can. kinetic terms for neutrinos only
conserves L!

Minimal unitarity violation:

All non-standard effects governed by (non-unitary) leptonic mixing matrix N



Consistent framework:
Can now be confronted
with experiment ...

→ talk by M. Blennow

Stefan Antusch
MPI für Physik (Munich)



Non-Unitarity and Leptogenesis

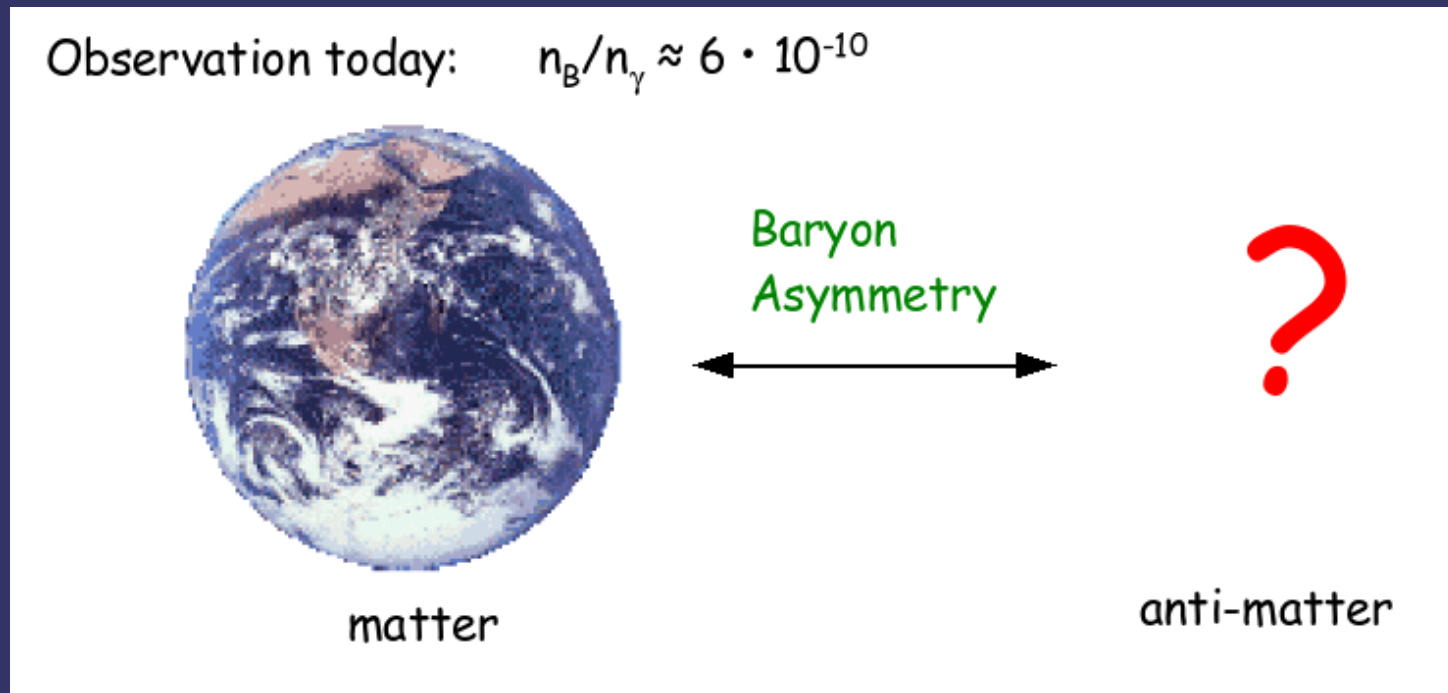


Non-Unitarity and Leptogenesis

- ➔ How does non-unitarity U_{PMNS} affect leptogenesis?
- ➔ *As we will see:* In 'low scale seesaw models' non-unitarity can lead to a strong enhancement of the decay asymmetries for leptogenesis!
- ➔ Can the non-unitarity of U_{PMNS} drive (testable) low scale leptogenesis?



Motivation: The baryon asymmetry of the universe

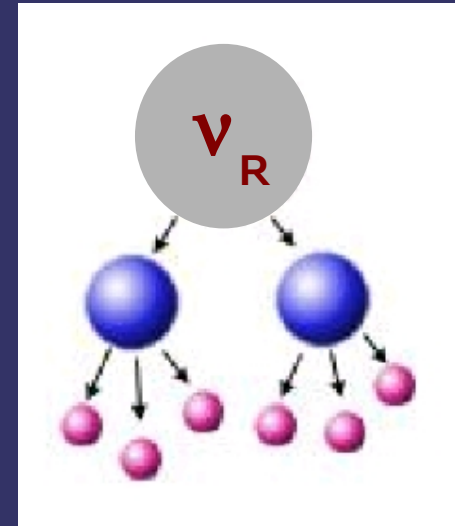


- ➔ How was the observed baryon asymmetry of the universe (BAU) generated?

Leptogenesis: The mechanism

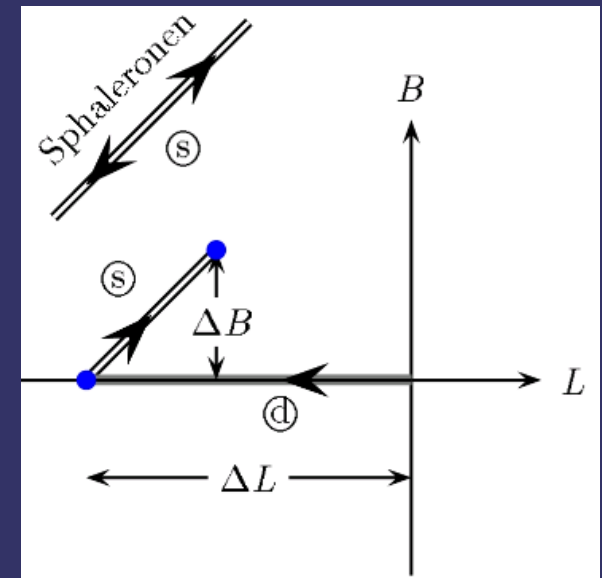
- Out-of-equilibrium decay of heavy fermionic singlets (RH neutrinos) in the early universe
⇒ lepton asymmetries ΔL_α

Fukugita, Yanagida ('86)



- Sphaleron processes (conserve $B - L$ but violate B and L) within SM (MSSM) partly convert lepton asymmetries into baryon asymmetry ΔB

Kuzmin, Rubakov, Shaposhnikov ('85)



SM + 'heavy' singlet fermions can explain neutrino masses and the baryon asymmetry!



How much baryon asymmetry is produced?

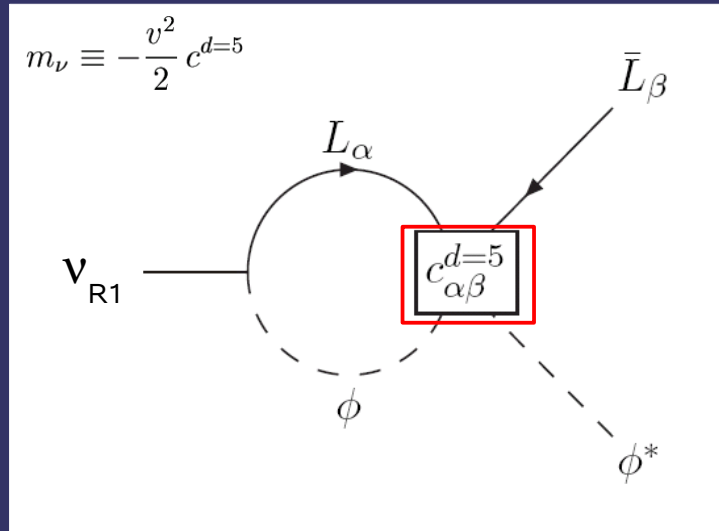
$$\text{BAU} \propto \sum_{\alpha} \eta_{\alpha} \varepsilon_{1,\alpha}$$

η_{α} : efficiency factors (from Boltzmann eqs., can be $O(1)$)

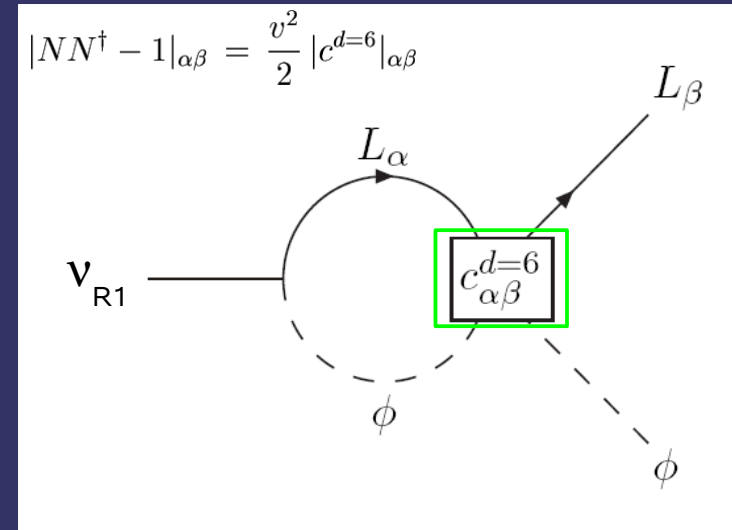
$\varepsilon_{1,\alpha}$: decay asymmetries (ν_R^1 into $L_{\alpha} + H$); interference of tree-level decay with loop-diagrams; assumed here: ν_R^1 dominates leptogenesis



Decay Asymmetries and Non-Unitarity (in effective theory)



related to neutrino masses!



related to non-unitarity!

$$\varepsilon_{1,\alpha} \simeq \frac{1}{8\pi(Y Y^\dagger)_{11}} \sum_{\beta} \left\{ \text{Im} \left[-\frac{3M'}{2} Y_{1\alpha}^* c_{\alpha\beta}^{d=5} Y_{\beta 1}^\dagger + M'^2 Y_{1\alpha} c_{\alpha\beta}^{d=6} Y_{\beta 1}^\dagger \right] \right\}$$

assumed: v_{R1} dominates; $M' = M_{\nu R1} \ll M_{\nu R2}, M_{\nu R3}$



Explicit example: minimal scenario

'Lepton number'
symmetry allowed
(leading order)

Lepton numbers
 $L_f: 1, N_1: 0, N_2: +1, N_3: -1$

$$Y_N = \begin{pmatrix} 0 & 0 & 0 \\ y_e & y_\mu & y_\tau \\ 0 & 0 & 0 \end{pmatrix}, \quad M^N = \begin{pmatrix} M' & 0 & 0 \\ 0 & 0 & M \\ 0 & M & 0 \end{pmatrix}$$

Non-unitarity!

$$c_{\alpha\beta}^{d=6} = \frac{y_\alpha^* y_\beta}{M^2}$$

unsuppressed
by symmetry

'Lepton number'
breaking terms
(L breaking small)

$$Y_N = \begin{pmatrix} \mu'_e & \mu'_\mu & \mu'_\tau \\ y_e & y_\mu & y_\tau \\ \mu_e & \mu_\mu & \mu_\tau \end{pmatrix}, \quad M^N = \begin{pmatrix} M' & \mu'_4 & \mu'_5 \\ \mu'_4 & \mu_4 & M \\ \mu'_5 & M & \mu_5 \end{pmatrix}$$

$$c_{\alpha\beta}^{d=5} \leftrightarrow m_\nu$$

suppressed by
symmetry



Explicit example: minimal scenario

'Lepton number' symmetry allowed (leading order)

$$Y_N = \begin{pmatrix} 0 & 0 & 0 \\ y_e & y_\mu & y_\tau \\ 0 & 0 & 0 \end{pmatrix}, \quad M^N = \begin{pmatrix} M' & 0 & 0 \\ 0 & 0 & M \\ 0 & M & 0 \end{pmatrix}$$

Non-unitarity!

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$$c_{\alpha\beta}^{d=5} \leftrightarrow m_\nu$$

suppressed by symmetry

$$\varepsilon_{1,\alpha} \simeq \frac{1}{8\pi(Y Y^\dagger)_{11}} \sum_\beta \left\{ \text{Im} \left[-\frac{3M'}{2} Y_{1\alpha}^* c_{\alpha\beta}^{d=5} Y_{\beta 1}^\dagger + M'^2 Y_{1\alpha} c_{\alpha\beta}^{d=6} Y_{\beta 1}^\dagger \right] \right\}$$

The d=6 contribution (\rightarrow non-unitarity) dominates flavoured decay asymmetries $\varepsilon_{1,\alpha}$! This is generic in 'low scale seesaw' with approximate lepton number!

S.A., Blanchet, Blenow, Fernandez-Martinez ('09)



Non-unitarity driven (testable) low scale leptogenesis?

... operating, e.g., at TeV energies?

- ➔ Promising: Decay asymmetries can be strongly enhanced!
- ➔ Note: Flavour effects (different efficiencies for different flavours are crucial, since $\sum_{1,\alpha} \epsilon_{1,\alpha}$ from d=6 operator vanished exactly)

$$\text{BAU} \propto \sum_{\alpha} \eta_{\alpha} \epsilon_{1,\alpha}$$

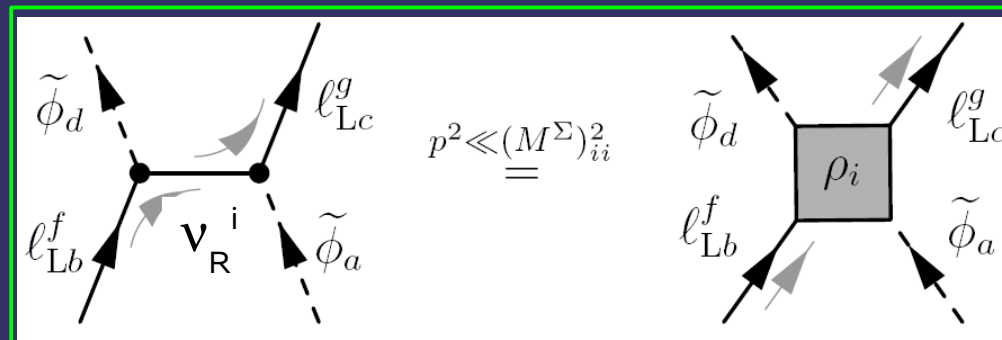
different factors for different
lepton flavours



However, non-unitarity has another important effect ...

- The d=6 operator for non-unitarity can also mediate **flavour equilibration in the thermal bath!**

S.A., Blanchet, Blennow, Fernandez-Martinez ('09)



- If **flavour equilibrating processes** dominate over the **flavour-dependent washout processes**, then the **d=6 operator** can **not** successfully drive leptogenesis!

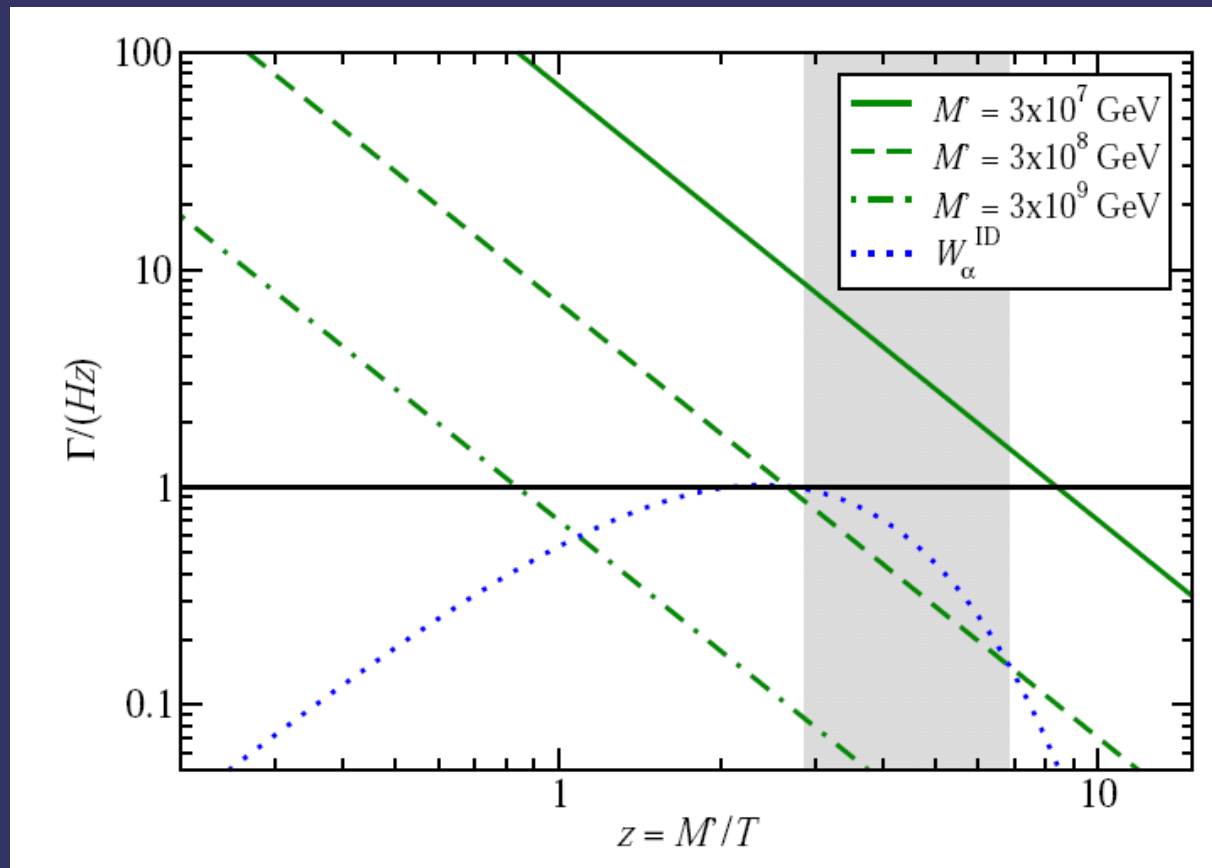
For other sources of flavour equilibration, see also:
Sierra, Losada, Nardi ('09)

Stefan Antusch
MPI für Physik (Munich)



In a minimal realisation of non-unitarity driven leptogenesis ...

S.A., Blanchet, Blennow, Fernandez-Martinez ('09)



- ➔ ... we find that TeV scale leptogenesis with observable non-unitarity is not possible (but, nevertheless, leptogenesis bound relaxed to $M' > 10^8$ GeV)

Brief Summary and Conclusions

→ Non-unitarity

- Typical signal of new physics in the lepton sector
- Minimal Unitarity Violation (MUV): Consistent minimal scheme

→ Leptogenesis and Non-unitarity

- Non-unitarity effects ($d=6$ operator) can strongly enhance the flavoured decay asymmetries for leptogenesis. Enhancement generic in low scale seesaw models with approximately conserved 'lepton number' symmetry!
- Additional effect: Same $d=6$ operator can mediate flavour equilibrating processes in the thermal bath
- Open question: Is there a well motivated model which realises low scale (testable) 'non-unitarity driven leptogenesis'?

